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HIER-GRP: A COMPUTER PROGRAM FOR THE HIERARCHICAL GROUPING OF R--ETC(U)
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HIER-GRP:

A COMPUTER PROGRAM FOR THE HIERARCHICAL
GROUPING OF REGRESSION EQUATIONS

By

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9/Final rept.

COMPUTATIONAL SCIENCES DIVISION

Brooks Air Force Base, Texas 78235

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This technical report has been reviewed and is approved for publication.

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PREFACE

This research was completed under project 6323, Personnel Data Analyses; task 632305, Development of Analytic Methodology for Air Force Personnel Research Data.

In addition to the acknowledgments expressed in the introduction section of this report, the author wishes to give special credit to Mr. William S. Mathon for his numerous and valuable contributions to this project. Mathon performed the majority of the necessary programming tasks and prepared the basic text for Appendix B. Others who deserve mention include Mr. Larry K. Whitehead and Ms. Deana J. Olden for programming modifications and A1C Susan E. Tobey and Ms. Doris E. Black for technical editing. Finally, appreciation goes to Ms Dorothy M. Cobern and Ms. Laurel J. Betz for typing and proofreading the draft report.

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HIER-GRP: A COMPUTER PROGRAM FOR THE HIERARCHICAL GROUPING OF REGRESSION EQUATIONS

I. INTRODUCTION

HIER-GRP, an acronym for hierarchical grouping, is a computer program which was developed for various Air Force research purposes at the Computational Sciences Division, Air Force Human Resources Laboratory, Brooks AFB, Texas. Given a starting set of k regression equations, each of which contains the same criterion and predictor variables, the basic objective of the HIER-GRP algorithm is to group or to cluster the equations in a stepwise or iterative manner so as to minimize the overall loss of predictive efficiency at each iteration. Initially there are k separate groups; i.e., each of the k equations is considered as a group by itself, and a measure of overall predictive efficiency is computed. At the first iteration all possible ways of combining any two of the equations from the total k equations are examined, and that combination providing the minimum loss of overall predictive efficiency is selected to form a "new group." Formation of the new group reduces the number of equations to $k-1$ for the start of the second iteration. The process continues until only one final group remains and is "hierarchical" in the sense that the pattern of the number of groups from start to finish is $k, k-1, k-2, \dots, 1$.

The mathematical theory upon which HIER-GRP is based is documented in an Air Force publication entitled *An Iterative Technique for Clustering Criteria Which Retains Optimum Predictive Efficiency* by Robert A. Bottenberg and Raymond E. Christal (3). Early developmental work was also accomplished by Joe H. Ward, Jr., (16), and some of the original programming was done by Daniel D. Rigney.

HIER-GRP or one of the earlier versions of the program has been used extensively by the Air Force in the past, especially in conjunction with "policy-capturing applications." Policy-capturing is a methodology composed of multiple linear regression analysis and hierarchical grouping procedures (1, 3, 4, 6, 7, 14, 16, 17, and 18). In this context, HIER-GRP was used in the development of the Weighted Airman Promotion System (WAPS) (10) and later in the reevaluation of WAPS (12 and 13). The program was also used in developing officer grade requirements (9), a promotion system for airman basics (2), a screening system for the Air Reserve Forces (8), and a senior NCO promotion system (11).

This report describes the technical details that are required for the use of the HIER-GRP program as it is currently operational on the Univac 1108 computer system at the Computational Sciences Division. The basic algorithm is first discussed, and the essential steps are outlined. Details of the computer system requirements and descriptions of necessary control cards are then presented. Next, the output of HIER-GRP is explained. Appendices are included that contain the mathematical formulas used in the program, some mathematical background helpful for understanding the algorithm, sample output, and a complete source card listing of the program.

Partly as a result of the research studies referenced above, requests for copies of the HIER-GRP computer program and associated documentation from different Air Force agencies, other governmental organizations, colleges, and universities have been numerous. Since 1969, approximately twenty copies of HIER-GRP have been provided to different requesters and implemented on a variety of different computer systems. One purpose of this report is to provide a document which can be used to satisfy any future requests for HIER-GRP.

II. BASIC ALGORITHM

This section describes the basic structure of the HIER-GRP algorithm. The reader is referred to Appendix A for computational formulas mentioned in the various steps and to Appendix B for more detailed mathematical considerations.

The basic steps of the HIER-GRP algorithm can be summarized as the following five phases: (a) data input and program termination, (b) computation of the overlap matrix, (c) determination of the order of clustering, (d) computation of the statistics for the initial k criteria, and (e) iteration to reduce the number of criteria. Each of these phases is described in the following steps. The steps are to be followed in numeric order unless indicated otherwise.

Steps 1-2. Data Input and Program Termination

1. Read "Problem Definition Card." This card defines k , the number of criteria or regression equations to be grouped and the number of standardized regression (beta) weights in each equation. If no Problem Definition Card is read, terminate the program.

2. Read in the number of cases, the criterion means and standard deviations, the standardized regression weights, the validities, and the predictor means and standard deviations for each equation. Assign each equation the identification numbers 1 through k , respectively, according to the order in which the equations were read.

Step 3. Computation of the Overlap Matrix

3. Compute the overlap matrix A , where each element a_{ij} denotes the decrease in overall predictive efficiency if equation i is combined with equation j ; for $i = 1, 2, \dots, k, j = 1, 2, \dots, k$, and $i \neq j$. The diagonal elements of A are undefined and the elements above the diagonal are symmetric with those elements below the diagonal.

Steps 4-8. Determination of the Order of Clustering

4. Set NGRPS, the index denoting the current number of groups, equal to k . Initially each criterion (equation) belongs to a separate cluster.

5. Considering all clusters present at the NGRPS stage, select two of the clusters denoted by i and j such that:

a. $a_{ij} \leq a_{\ell m}$ where ℓ and m are the identification numbers of any cluster present at the NGRPS stage and $\ell \neq m$, and

b. $i < j$. This can be accomplished by examining the elements above the diagonal of the overlap matrix and selecting the smallest element.

6. Form a new criterion cluster from the old clusters i and j identified in Step 5. Record the identifications of the two clusters i and j in the storage areas IU_{NGRPS} and JU_{NGRPS} , respectively. Assign the new cluster the identification number i .

7. Decrement NGRPS by 1. If $NGRPS > 1$, go to Step 8; otherwise proceed to Step 9.

8. Update the overlap matrix as follows. For each $\ell, \ell \neq i$ of Step 6 where ℓ is the identification number of a criterion cluster present at the NGRPS stage, compute the decrease in overall predictive efficiency if equation ℓ is combined with equation i . Since NGRPS was reduced by 1 in Step 7, the dimension of the updated overlap matrix will be reduced by 1. Return to Step 5.

Step 9. Computation of the Statistics for the Initial k Criteria

9. Compute the squared multiple correlation coefficient for each of the initial k regression equations and, also, ORU_k , the overall squared multiple correlation coefficient obtained by considering a regression model with no grouping of initial equations.

Steps 10–15. Iteration to Reduce the Number of Criteria

10. Form an initial grouping of the k equations by assigning each equation to a group by itself. This is the “ k groups” stage. Set $NGRPS$ equal to k .

11. Form a new grouping of the k equations by following the grouping order established in Steps 4–8. This is accomplished by combining the groups identified by IU_{NGRPS} and JU_{NGRPS} and assigning the new group (criterion cluster) the identification number in IU_{NGRPS} .

12. Compute the least squares regression equation which can be used to predict the new group and decrement $NGRPS$ by 1.

13. Print all statistics concerning the new grouping including:

- a. the identification numbers of the two equations combined at this iteration,
- b. An F value testing the difference between the prediction equations for the two clusters in (a),
- c. An F value testing the difference between the k initial prediction equations and the smaller set of $NGRPS$ equations (one for each cluster) used at the “ $NGRPS$ groups” stage, and
- d. the overall squared multiple correlation coefficient obtained using the $NGRPS$ equations at this stage.

14. Print a summary of all groups (clusters) present at the $NGRPS$ stage. Also, print the prediction equation for the new group (including standardized and raw score weights).

15. If $NGRPS > 1$, loop back to Step 11; otherwise, return to Step 1 and begin the next problem.

III. DESCRIPTIONS OF THE HIER-GRP PROGRAM

Systems Requirements

The HIER-GRP program is composed of seven routines—the main or driver routine and six subroutines. The entire program, with the exception of the Univac Assembly Language subroutine `START`, is written in FORTRAN IV. The assembly subroutine `START` is called once at the beginning of the driver routine and is never called again. Its only function is to reset the margin control on the Univac 1108 printer.

The Univac version of FORTRAN has a special statement, the Parameter statement, which is used in the driver routine and which may not be available on other computers. The Parameter statement is used to define the dimensions of arrays at compilation time. The Parameter statement can be removed if each array is dimensioned to its required size.

The complete HIER-GRP program requires approximately 10,000 36-bit words of core storage in addition to the number of words required for arrays. If P is the number of predictors and E is the number of equations, then the amount of storage required for arrays is $12E+3P+2 \cdot E \cdot P + [E \cdot (E-1)/2] + 14$. For example, if $P = 50$ and $E = 50$, then 6,989 words of storage are required for arrays.

There are a total of 1,121 cards in the HIER-GRP program deck. Of these, only 601 are source language cards and the remainder are comments cards. The number of cards and the intrinsic system routines required in each of the seven routines which make up HIER-GRP are listed in Table 1.

Table 1. Characteristics of the HIER-GRP Routines

Program Name	Source Language	Number of Source Language Cards	Number of Comment Cards	Intrinsic System Routines Required
DRIVER (MAIN)	FORTRAN IV	100	311	None
START	ASSEMBLY	7	0	None
OVRLP	FORTRAN IV	36	36	None
GROUP	FORTRAN IV	76	48	None
STAGE	FORTRAN IV	81	42	None
PRINTG	FORTRAN IV	218	82	SQRT
PLEVEL	FORTRAN IV	83	1	ATAN, SQRT, ALOG, EXP, SIN

Data Requirements

A HIER-GRP user must supply the following data for each regression equation:

1. The number of cases (N) which were used to compute the equation
2. The criterion mean and standard deviation (SD)
3. The standardized regression weights
4. The validity coefficients (correlations of predictor or independent variables with the criterion or dependent variable)
5. The predictor means and standard deviations.

The computational formulas developed by Bottenberg and Christal (3) and used within the program assume that the predictor sums-of-squares and cross-products matrices are proportional; i.e., that the ratios of the corresponding elements of the sums-of-squares and cross-products matrices for any two equations to be clustered are equal to the ratio of the corresponding numbers of the cases within each equation. This assumption of proportionality is discussed in detail by Bottenberg and Christal (1961, see pages 8 through 11) and also addressed in Appendix B (see equation 9b) of this report. In practice this assumption is met by selecting items (1) and (5) of the previous paragraph to be identical for each equation.

Run-Stream Organization

The following card sequence is required to use the HIER-GRP program as it is operational on a Univac 1108 computer:

- | Order | Card Type |
|-------|---|
| 1. | @RUN |
| 2. | @XQT T*T.HIER-GRP |
| 3. | Problem Definition Card |
| 4. | Header Card(s) |
| 5. | Format Card for Equation Ns |
| 6. | Data Card(s) - Equation Ns |
| 7. | Format Card for Criterion Means and SDs |
| 8. | Data Card(s) - Criterion Means and SDs |
| 9. | Format Card for Beta Weights |
| 10. | Data Card(s) - Beta Weights |
| 11. | Format Card for Validities |

12. Data Card(s) – Validities
13. Format Card for Predictor Means and SDs
14. Data Card(s) – Predictor Means and SDs
15. The sequence of cards 3–14 is required for each run.
As many problems as desired may be run by stacking one problem after another.
16. Blank Card to Terminate Run
17. @FIN

The Univac 1108 System Cards (1, 2, and 17) are described in the Univac Exec 8 Reference Manual (15). Descriptions of cards 3–16 are presented in the next section. See Appendix C for sample run-stream and sample control cards.

Control Cards

Problem Definition Card

Card Columns	FORTRAN Format		Description
1–3	I3	NEQS,	the number of criteria (systems, regression equations) in this problem. NEQS must be less than or equal to 50.
4–6	I3	NPREDs,	the number of beta weights (standardized regression weights) in each equation. NPREDs must be less than or equal to 100.
7	I1	IOPT,	the grouping (clustering) option desired. Normally a “6” is specified which causes the grouping to be done based on the iterative technique developed by Bottenberg and Christal (3). Other options are included in the program and comments cards, but are for future developmental purposes only.
8	I1	NHDRS,	the number of header (label, title) cards that follow this control card. Header cards can be omitted (NHDRS = 0) or up to 9 cards may be specified.
9	I1	IREAD,	the data read option. IREAD = 0 means read the beta weights and validities NPREDs items at a time. IREAD = 1 means read them NEQS*NPREDs items at a time. IREAD allows flexibility in the format of input data. However, IREAD is normally set equal to zero.
10–80			These card columns are not read.

Header Cards

Each header card will be printed only once at the beginning of the grouping report. Exactly NHDRS header cards must be present.

Format and Data Cards

1. *Format Card for Equation Ns.* This card supplies the FORTRAN variable format by which the number of cases used in the computation of each equation is to be read. Only the F and X editing codes are permitted.
2. *Data Card(s) – Equation Ns.* These cards are read according to the previous format card. The number of cards required depends on the format specifications.
3. *Format Card for Criterion Means and SDs.* This card provides the FORTRAN variable format by which the criterion mean and standard deviation for each equation are to be read. Only the F and X editing codes are permitted.
4. *Data Card(s) – Criterion Means and SDs.* These cards are read according to the previous format card. The number of cards required depends on the format specifications.
5. *Format Card for Beta Weights.* This card supplies the FORTRAN variable format by which the beta weights (NPREDs weights per equation) are to be read. Only the F and X editing codes are permitted.
6. *Data Card(s) – Beta Weights.* These cards are read according to the previous format card. Exactly NEQS sets of cards are required if IREAD = 0. The first set contains the beta weights for equation 1; the second set contains the beta weights for equation 2; and so on. The number of cards within each set depends on the format specifications.
7. *Format Card for Validities.* This card provides the FORTRAN variable format by which the validity coefficients for each equation are read. Only the F and X editing codes are permitted.
8. *Data Card(s) – Validities.* These cards are read according to the previous format card. Exactly NEQS sets of cards are required if IREAD = 0. The first set contains the validities for equation 1; the second set contains the validities for equation 2; and so on. The number of cards within each set depends on the format specifications.
9. *Format Card for Predictor Means and SDs.* This card supplies the FORTRAN variable format by which the predictor means and standard deviations for each equation are to be read. Only the F and X editing codes are permitted.
10. *Data Card(s) – Predictor Means and SDs.* These cards are read according to the previous format card. The number of cards required depends on the format specifications.

Output

The printed output of HIER-GRP is divided into five parts — the monogram and version date, the control card parameters, the problem header label, the format and input data cards, and the criterion grouping results. Each of these divisions is described in the following paragraphs. Refer to Appendix C for sample output.

Monogram and Version Date

The program title "Hierarchical Grouping Program HIER-GRP," the AFHRL monogram, and the program version date are printed at the beginning of each problem. The program version date is the last time the program was updated or modified.

Control Card Parameters

The parameters specified on the Problem Definition card are printed under the heading CONTROL CARD PARAMETERS. This includes the number of regression equations (criteria), the number of beta weights in each equation, the grouping option desired, and the number of header cards for this problem.

Problem Header Label

The problem header label, if header cards were specified on the Problem Definition Card, is printed under the heading PROBLEM HEADER LABEL.

Format and Input Data Cards

All format cards and all input data are printed under the heading FORMAT CARDS AND INPUT DATA. First, the format statements used to read the number of cases and the criterion means and standard deviations for each equation are printed. A table listing the equation numbers, the number of cases, the criterion means, and the criterion standard deviations is printed next. Third, the format statement used to read the beta weights and a table listing the equation number and the beta weights (15 per line) for each equation are printed. Fourth, the format statement used to read the validity coefficients, and a table listing the equation number and the validities (15 per line) for each equation are printed. Finally, the format statement used to read the predictor means and standard deviations and a table listing the predictor variable number and predictor means and standard deviations (one each per line) are printed.

Criterion Grouping Results

The results of the clustering process are printed under the heading HIERARCHICAL GROUPING RESULTS. The output in this division can be separated into three parts – the grouping option description, the R-square (RSQ) summary for the NEQS initial criteria, and the results of each iteration. Each of these sections is described as follows.

1. *Grouping Option Description.* The grouping option and a verbal description of the grouping option specified on the Problem Definition Card are printed.
2. *RSQ Summary for the NEQS Initial Criteria.* The number, NEQS, of initial criteria; the overall RSQ, ORU_{NEQS} , achieved by using the beta weights specified on the input data cards; and a table listing the equation number and the RSQ for each equation are printed.
3. *Results of Each Iteration.* The statistics and tables printed at each iteration, i.e., the information printed below each row of asterisks is listed as the following in Table 2.

Table 2. Output for Each Iteration

Computer Output Label	Meaning
Stage = ℓ	ℓ is the number of criterion clusters present at the end of this iteration.
OVERALL RSQ = ORU_{ℓ}	This is the RSQ obtained by using ℓ equations (one for each criterion cluster present at this stage) to predict the NEQS initial criteria.
SYSTEMS GROUPING THIS STAGE Table	
SYS IDENT	The identification (ID) numbers of the two criterion clusters combined at this iteration.
NO. MEMBERS	The number of members in each criterion cluster. The ID numbers of the members of each cluster can be obtained by referring to the summary roster for stage $\ell+1$.
NO. CASES	The number of cases used in the computation of the prediction equation for each criterion cluster. This number is the sum of the number of cases used in the prediction equation for each member of the cluster.
RSQ	The squared multiple correlation coefficient which is obtained by predicting each criterion within a cluster from the same compromise regression equation.
DECISION VALUE	The loss associated with replacement of the two clusters combined at this stage.
F-TEST FOR THE EQUALITY OF REGRESSION PARAMETERS FOR SYS'S COMBINED AT THIS STAGE Table	This table outlines a test of the hypothesis that the prediction equations for the two criterion clusters combined at this stage are identical. Equivalently, it is a test of the loss in predictive efficiency when each criterion within the two clusters combined at this stage are predicted from the same compromise equation.
CHANGE FROM $\ell+1$ SYSTEMS	
RSQ = $ORU_{\ell+1} - ORU_{\ell}$	The decrease in OVERALL RSQ from stage $\ell+1$.
DF = $NPREDs+1$	The decrease in the number of parameters estimated from stage $\ell+1$.
RESIDUAL	
RSQ = $1 - ORU_{\ell+1}$	The proportion of the criterion variance attributable to error at stage $\ell+1$.
DF = $N - (\ell+1)(NPREDs+1)$	The total number of cases less the number parameters estimated at stage $\ell+1$. Equivalently, DF is the number of degrees of freedom associated with the error portion of the criterion variance at stage $\ell+1$.
FSTAT = $\frac{[(ORU_{\ell+1} - ORU_{\ell})/(NPREDs+1)]}{[(1 - ORU_{\ell+k})/(N - (\ell+1)(NPREDs+1))]}$	The F statistic testing the hypothesis described in the preceding paragraph (FOR SYS'S COMBINED AT THIS STAGE)

Table 2. (Continued)

Computer Output Label	Meaning
SIG LVL	The probability that a value of the F statistic greater than FSTAT would occur by chance. A value of SIG LVL equal to α means that if the hypothesis being tested is true, then a value of the F statistic greater than FSTAT would have occurred 100 α percent of the time by chance. Therefore, small values of α tend to reject the hypothesis being tested.
F-TEST FOR THE EQUALITY OF REGRESSION PARAMETERS FOR SYS'S COMBINED UP TO THIS STAGE Table	This table outlines a test of the hypothesis that the prediction equations for all members of criterion cluster number 1 are identical, the prediction equations for all members of criterion cluster 2 are identical, and so on for the ℓ criterion clusters present at the end of this iteration. Equivalently, this tests the loss in predictive efficiency when ℓ equations (one for each criterion cluster) are used to predict the NEQS initial criteria instead of the original NEQS equations.
CHANGE FROM NEQS SYSTEMS	
$RSQ = ORU_{NEQS} - ORU_{\ell}$	The decrease in OVERALL RSQ from stage NEQS.
$DF = (NEQS - \ell)(NPRED + 1)$	The decrease in the number of parameters estimated from stage NEQS.
RESIDUAL	
$RSQ = 1 - ORU_{NEQS}$	The proportion of the criterion variance attributable to error at stage NEQS.
$DF = N - (NEQS)(NPRED + 1)$	The total number of cases less the number of parameters estimated at stage NEQS. Equivalently, DF is the number of degrees of freedom associated with the error portion of the criterion variance at stage NEQS.
$FSTAT = [(ORU_{NEQS} - ORU_{\ell}) / (NEQS - \ell)(NPRED + 1)] / [(1 - ORU_{NEQS}) / (N - (NEQS)(NPRED + 1))]$	The F statistic testing the hypothesis described in the preceding paragraph (FOR SYS'S COMBINED UP TO THIS STAGE)
SIG LVL	The probability that a value of the F statistic greater than FSTAT would occur by chance. A value of SIG LVL equal to α means that if the hypothesis being tested is true, then a value of the F statistic greater than FSTAT would have occurred 100 α percent of the time by chance. Therefore, small values of α tend to reject the hypothesis being tested.
SYSTEMS SUMMARY ROSTER Table	The summary roster is a listing of all the criterion clusters present at the end of the current iteration. The members and the RSQ for each cluster are also printed. In addition, the prediction equation and the system mean and standard deviation for the new criterion cluster formed at the present iteration are printed. The compromise equation for each criterion cluster present at a given iteration can be obtained by referring to the summary roster for the stage at which the cluster was formed.

Table 2. (Continued)

Computer Output Label	Meaning
STAGE IDENT	The stage at which each criterion cluster was formed.
SYS LOSS	The contribution of each criterion cluster to the decrease in OVERALL RSQ from stage NEQS. Equivalently, this is the amount by which the OVERALL RSQ would increase if each of the criteria within this cluster were predicted from their individual regression equations rather than from the compromise equation for the cluster.
NO. MEMBERS	The number of criteria within each criterion cluster. The ID numbers of the members of each cluster are listed under the headings SYS IDENT and IDENTIFICATION OF OTHER MEMBERS in this table.
RSQ	The squared multiple correlation coefficient which is obtained by predicting each criterion within a cluster from the same compromise regression equation.
NO. CASES	The number of cases used in the computation of the compromise equation for a criterion cluster. This number is the sum of the number of cases used to compute the regression equation for each criterion within the cluster.
SYS IDENT	The ID number of a criterion cluster. This is also the smallest ID number of the criteria within this cluster.
IDENTIFICATION OF OTHER MEMBERS	The ID numbers of the remaining criteria within a cluster.
NEW SYS CRITERION MEAN	The criterion mean for the cluster formed at this iteration.
NEW SYS CRITERION SD	The criterion standard deviation for the cluster formed at this iteration.
BETA WEIGHTS FOR THE NEW SYSTEM S	The values (10 per line) of the least squares standardized regression coefficients for the regression equation which is the best single predictor for all the criteria in the new cluster where S is the ID number of the new cluster. Equivalently, these are the beta weights which would be obtained by pooling the observations for all the criteria in the new cluster and computing the regression of the pooled criteria on the NPREDs predictor variables.
RAW SCORE WEIGHTS FOR THE NEW SYSTEM S	The values (5 per line) of the raw score weights for the regression equation which is the best single predictor for all the criteria in the new cluster S.
REGRESSION CONSTANT	The regression constant for the regression equation which is the best single predictor of all the criteria in the new cluster.
Y SINGLE MEMBER SYSTEMS	A list of the identification numbers of the "Y" single criteria which have not been combined with any system up to this stage.

REFERENCES

1. **Anderberg, M.R.** *Cluster analysis for applications*. OAS-TR-72-1, AD-738-301. Kirtland AFB, NM: Office of the Assistant for Study Support, January, 1972.
2. **Black, D.E.** *Development of the E-2 weighted airman promotion system*. AFHRL-TR-73-3, AD-767 195. Lackland AFB, TX: Personnel Research Division, Air Force Human Resources Laboratory, April 1973.
3. **Bottenberg, R.A., & Christal, R.E.** *An interactive technique for clustering criteria which retains optimum predictive efficiency*. WADD-TN-61-30, AD-261 615. Lackland AFB, TX: Personnel Laboratory, Wright Air Development Division, March 1961. Also, *Journal of Experimental Education*, Summer 1968, 36(4), pp. 28-34.
4. **Bottenberg, R.A., & Ward, J.H., Jr.** *Applied multiple linear regression*. PRL-TDR-63-6, AD-413 128. Lackland AFB, TX: 6570th Personnel Research Laboratory, Aerospace Medical Division, March 1963.
5. **Brown, B.** Simple comparisons of simultaneous regression lines. *Biometrics*, 1970, 26, pp. 143-144.
6. **Christal, R.E.** *JAN: A technique for analyzing group judgment*. PRL-TDR-63-3, AD-403 813. Lackland AFB, TX: 6570th Personnel Research Laboratory, Aerospace Medical Division, February 1963.
7. **Christal, R.E.** *Selecting a harem--and other applications of the policy-capturing model*. PRL-TDR-67-1, AD-658 025. Lackland AFB, TX: Personnel Research Laboratory, Aerospace Medical Division, March 1967.
8. **Gott, C.D.** *Development of the weighted airman screening system for the air reserve forces*. AFHRL-TR-74-18, AD-781 747. Lackland AFB, TX: Computational Sciences Division, Air Force Human Resources Laboratory, March 1974.
9. **Hazel, J.T., Christal, R.E., & Hoggatt, R.S.** *Officer grade requirements project: IV. Development and validation of a policy equation to predict criterion board ratings*. PRL-TR-66-16, AD-659 125. Lackland AFB, TX: Personnel Research Laboratory, Aerospace Medical Division, November 1966.
10. **Koplyay, J.B.** *Field test of the weighted airman promotion system: Phase I. Analysis of the promotion board component in the weighted factors system*. AFHRL-TR-69-101, AD-689 751. Lackland AFB, TX: Personnel Research Division, Air Force Human Resources Laboratory, April 1969.
11. **Koplyay, J.B., Albert, W.G., & Black, D.E.** *Development of a senior NCO promotion system*. AFHRL-TR-76-48, AD-A030 607. Lackland AFB, TX: Computational Sciences Division, Air Force Human Resources Laboratory, July 1976.
12. **Koplyay, J.B., & Gott, C.D.** *Reevaluation of the operational weighted airman promotion system for grades E-5 through E-7*. AFHRL-TR-73-25, For Official Use Only. Lackland AFB, TX: Computational Sciences Division, Air Force Human Resources Laboratory, November 1973.
13. **Koplyay, J.B., & Gott, C.D.** *Revalidation of the factors which comprise the E-5/E-7 weighted airman promotion system (WAPS)*. AFHRL-TR-77-80, For Official Use Only. Brooks AFB, TX: Computational Sciences Division, Air Force Human Resources Laboratory, December 1977.
14. **Martin, F.B., & Zyskind, G.** On Combinability of Information from Uncorrelated Linear Models by Simple Weighting. *Annals of Mathematical Statistics*, Aug-Dec 1966, 37, pp. 1338-1347.
15. **Sperry Rand Corporation.** Univac 1100 Series Operating System, Programmer Reference, UP-4144 Rev. 3, 1974.
16. **Ward, J.H., Jr.** *Hierarchical Grouping to Maximize Payoff*. WADD-TN-61-29, AD-261 750. Lackland AFB, TX: Personnel Laboratory, Wright Air Development Division, March 1961.
17. **Welch, B.L.** Some problems in the analysis of regression among K samples of two variables. *Biometrika*, 1935, 27, pp. 145-160.
18. **Wilson, J.W., & Carry, L.R.** Homogeneity of regression - its rationale, computation, and use. *American Educational Research Journal*, 1969, 6, pp. 80-90.

BIBLIOGRAPHY

1. **Carter, A.H.** The estimation and comparison of residual regressions where there are two or more related sets of observations. *Biometrika*, 1949, 36, pp. 26-46.
2. **Chaud, U.** Distributions related to comparison of two means and regression coefficients. *Annals of Mathematical Statistics*, 1950, 21, pp. 507-521.
3. **Chipman, J.S., & Rao, M.M.** The treatment of linear restrictions in regression analysis. *Econometrica*, Jan-Apr 1964, 132(1-2), pp. 198-209.
4. **Fraser, A.S.** The Behrens-Fisher problem for regression coefficients. *Annals of Mathematical Statistics*, 1953, 24, pp. 390-402.
5. **Geeslin, W.E.** Comment on homogeneity of regression. *American Educational Research Journal*, 1970, 7, pp. 636-638.
6. **Kendall, M.G., & Stuart, A.** *The advanced theory of statistics*, Vol. 2, *Inference and relationship* (Vol. 2), New York: Hafner, 1961.
7. **Kullback, S., & Rosenblatt, H.M.** On the analysis of multiple regression in K categories. *Biometrika*, 1957, 44, pp. 67-83.
8. **Rao, C.R.** *Linear statistical inference and its applications*. New York: Wiley, 1965.
9. **Robson, D.S., & Aikinson, G.F.** Individual degrees of freedom for testing homogeneity of regression coefficients in a one-way analysis of covariance. *Biometrics*, 1960, 16, pp. 593-605.
10. **Theil, H.** *Principles of econometrics*. New York: Wiley, 1970.
11. **Williams, E.G.** *Regression analysis*. New York: Wiley, 1959.

APPENDIX A: NOTATION AND COMPUTATIONAL FORMULAS

The transpose of the associated matrix.

- k , The initial number of criteria.
 p , The number of variables.
 n_i , The number of cases used in the computation of the regression equation for criterion i .
 m_i , The mean for criterion i .
 σ_i^2 , The variance for criterion i .
 $\hat{\alpha}_i$, The constant term in the regression equation for criterion i .
 \hat{b}_i , The $p \times 1$ vector of regression weights for criterion i .
 $\hat{\beta}_i$, The $p \times 1$ vector of standard regression weights for criterion i .
 c_i , The $p \times 1$ vector of validities (intercorrelations between the criterion and the p independent variables) for criterion i .
 N , The total number of cases $N = n_1 + n_2 + \dots + n_k$
 m_0 , The pooled criterion mean $Nm_0 = n_1 m_1 + n_2 m_2 + \dots + n_k m_k$
 σ_0^2 , The pooled criterion variance

$$N\sigma_0^2 = n_1(\sigma_1^2 + m_1^2) + \dots + n_k(\sigma_k^2 + m_k^2) - Nm_0^2$$

- g_I , The number of criteria in cluster I .
 I , The set of criteria in cluster I . $I = \{i_1, i_2, \dots, i_{g_I}\}$. In the succeeding definitions, let I be the union of clusters J and L , $J \cup L$.
 N_I , The number of cases used in the computation of the composite equation for cluster I .

$$N_I = \sum_{i \in I} n_i = N_J + N_L$$

- M_I , The criterion mean for cluster I .

$$N_I M_I = \sum_{i \in I} n_i m_i = N_J M_J + N_L M_L$$

- σ_I^2 , The criterion variance for cluster I .

$$N_I \sigma_I^2 = \sum_{i \in I} n_i (\sigma_i^2 + m_i^2) - N_I M_I^2 = N_J (\sigma_J^2 + M_J^2) + N_L (\sigma_L^2 + M_L^2) - N_I M_I^2$$

- $\hat{\alpha}_I$, The constant term in the regression equation for cluster I .

$$N_I \hat{\alpha}_I = \sum_{i \in I} n_i \hat{\alpha}_i = N_J \hat{\alpha}_J + N_L \hat{\alpha}_L$$

- \hat{b}_I , The $p \times 1$ vector of regression weights for cluster I .

$$N_I \hat{b}_I = \sum_{i \in I} n_i \hat{b}_i = N_J \hat{b}_J + N_L \hat{b}_L$$

$\hat{\beta}_I$, The $p \times 1$ vector of standard regression weights for cluster I.

$$N_I \sigma_I \beta_I = \sum_{i \in I} n_i \sigma_i \hat{\beta}_i = N_J \sigma_J \beta_J + N_L \sigma_L \hat{\beta}_L$$

c_I , The $p \times 1$ vector of validities for cluster I.

$$N_I \sigma_I c_I = \sum_{i \in I} n_i \sigma_i c_i = N_J \sigma_J c_J + N_L \sigma_L c_L$$

R_i^2 , The squared multiple correlation coefficient for the regression on criterion i.

$$R_i^2 = \hat{\beta}_i' c_i$$

R_I^2 , The squared multiple correlation coefficient for the regression on cluster I.

$$R_I^2 = \hat{\beta}_I' c_I = \frac{1}{N_I \sigma_I^2} \left[N_J^2 \sigma_J^2 R_J^2 + N_L^2 \sigma_L^2 R_L^2 + N_J N_L \sigma_J \sigma_L (\hat{\beta}_J' c_L + \hat{\beta}_L' c_J) \right]$$

G_s , The set of s criterion clusters present at the s cluster stage.

$$G_s = \{ I_1, I_2, \dots, I_s \}.$$

${}_s R^2$, The squared multiple correlation coefficient for the criterion grouping, G_s , at the s cluster stage.

$$N \sigma_0^2 {}_s R^2 = \sum_{I \in G_s} N_I (\sigma_I^2 R_I^2 + M_I^2) - N m_0^2$$

Let $G_s = \{ J, L, K_3, \dots, K_s \}$ and

$G_{s-1} = \{ J \cup L, K_3, \dots, K_s \}$ then

$${}_s R^2 - {}_{s-1} R^2 = \frac{N_J N_L}{N \sigma_0^2 (N_J + N_L)} \left[\sigma_J^2 R_J^2 + \sigma_L^2 R_L^2 + (M_J - M_L)^2 - \sigma_J \sigma_L (\hat{\beta}_J' c_L + \hat{\beta}_L' c_J) \right]$$

APPENDIX B: MATHEMATICAL BACKGROUND

Mathematical Model for the Clustering Algorithm

Suppose that a set of p independent variables, $v' = (v_1, \dots, v_p)$, are linearly related to the expected values of each of k criteria, Y_1, \dots, Y_k ; that is,

$$(1) \quad E(Y_i|v) = v'b_i + \alpha_i \quad \text{for } i=1, \dots, k$$

where b_i is a $p \times 1$ vector of unknown population parameters and α_i is an unknown population constant. Let y_i be an $n_i \times 1$ vector of independent observations on criterion Y_i , let X_i be an $n_i \times p$ matrix of observations on the set of p independent variables v , where the j -th element of y_i corresponds to the j -th row of X_i , and let u_i be an $n_i \times 1$ vector in which each element is 1. Then from (1),

$$(1a) \quad E(y_i|X_i) = X_i b_i + u_i \alpha_i \quad \text{for } i=1, \dots, k.$$

Let $N = n_1 + \dots + n_k$; let $Y' = [y_1', \dots, y_k']$, the $1 \times N$ vector obtained by pooling all the criterion observations; let

$$X = \begin{bmatrix} u_1 X_1 & 0 & 0 & \dots & 0 \\ 0 & u_2 X_2 & 0 & \dots & 0 \\ 0 & \dots & \dots & \dots & u_k X_k \end{bmatrix}$$

the $N \times k(p+1)$ block diagonal matrix obtained by placing the $n_i \times (p+1)$ matrix of observations $[u_i X_i]$ in the i -th block diagonal position, and let $b' = [\alpha_1 b_1' \dots \alpha_k b_k']$, the $k(p+1)$ vector of unknown parameters. Under the assumption that the criterion observations are independent and have common variance, the mathematical model for the clustering algorithm is

$$(1b) \quad E(Y|X) = Xb \text{ with } D(Y|X) = \sigma^2 I,$$

where $D(Y|X)$ is the dispersion matrix of the criterion observations, σ^2 is the common variance, and I is the $N \times N$ identity matrix.

Minimum Variance Unbiased Estimation and Hypothesis Testing

The $k(p+1) \times 1$ vector b of unknown parameters in (1b) correspond to the k equations in (1a). The minimum variance unbiased estimates (mvue), $\hat{\alpha}_i$ and \hat{b}_i , of α_i and b_i are obtained from (1b) by the method of least squares, where

$$(2) \quad \begin{aligned} \hat{b}_i &= [X_i' X_i - \frac{1}{n_i} X_i' u_i u_i' X_i]^{-1} [X_i' y_i - \frac{1}{n_i} X_i' u_i u_i' y_i] \\ \hat{\alpha}_i &= \frac{1}{n_i} u_i' y_i - \frac{1}{n_i} u_i' X_i \hat{b}_i \end{aligned} \quad \text{for } i=1, \dots, k.$$

These are the estimates that would be obtained by the method of least squares from the k separate models

$$(3) \quad E(y_i | X_i) = X_i b_i + u_i \alpha_i \text{ with } D(y_i | X_i) = \sigma^2 I \quad \text{for } i=1, \dots, k$$

where the error variance, σ^2 , is the same for each model. It might be that some or all of the equations in (1) are identical. The technique of homogeneity of regression can be used to test the equality of vectors of regression parameters across several criteria. Chipman and Rao (1964) and Theil (1970) have developed methods for obtaining mvue under general linear restrictions and for testing general linear hypotheses. Rao (1965, pp 189-190) shows that in the case

$$(4) \quad E(Y | X) = Xb \text{ with } D(Y | X) = \sigma^2 I,$$

where X is $n \times s$ of rank s and b is $s \times 1$, the mvue, \hat{b}_Ψ , for b under the linear restriction

$$(4a) \quad \Psi b = 0 \text{ is}$$

$$(4b) \quad \hat{b}_\Psi = B(B'X'XB)^{-1}B'X'Y$$

where Ψ is $r \times s$ of rank r , B is $s \times (s-r)$ of rank $(s-r)$, and $\Psi B = 0$. Rao obtains this result by introducing the general solution, $B\theta$, where θ is an $(s-r) \times 1$ vector of new parameters, of (4a) into (4) to obtain the model

$$(5) \quad E(Y|X) = XB\theta \text{ with } D(Y|X) = \sigma^2 I$$

and no restrictions on θ . The mvue, $\hat{B}\hat{\theta}$, of $B\theta$ is $\hat{B}\hat{\theta}$ (see Rao, 1965, pp. 181-182), where $\hat{\theta}$ is the mvue of θ in (5). If, in addition to (4), Y has a multivariate normal distribution, then Chipman and Rao develop an expression for an unbiased critical region of size θ for the following hypothesis:

$$(6) \quad \Psi_1 b = 0 \text{ given that } \Psi_0 b = 0$$

where Ψ_1 is $r_1 \times s$ of rank r_1 , Ψ_0 is $r_0 \times s$ of rank r_0 , and $\Psi' = [\Psi_0' \Psi_1']$ is $s \times (r_0 + r_1)$ of rank $(r_0 + r_1)$. The expression for the unbiased critical region of size θ is

$$(7) \quad \left\{ F|F = \left(\frac{n-s+r_0}{r_1} \right) \left(\frac{EXSS}{ESSH} \right) = \left(\frac{n-s+r_0}{r_1} \right) \left(\frac{R_{\Psi_0}^2 - R_{\Psi}^2}{1 - R_{\Psi_0}^2} \right) > F_{\theta} \left(r_1, n-s+r_0 \right) \right\},$$

where $F_{\theta}(r_1, n-s+r_0)$ is the upper 100 $(1-\theta)\%$ point of the central F distribution with r_1 and $n-s+r_0$ degrees of freedom, and

$$ESSH = (Y - X\hat{b}_{\Psi_0})'(Y - X\hat{b}_{\Psi_0}),$$

$$EXSS = (Y - X\hat{b}_{\Psi})'(Y - X\hat{b}_{\Psi}) - ESSH,$$

\hat{b}_{Ψ_0} is the mvue of b under the restriction $\Psi_0 b = 0$,

\hat{b}_{Ψ} is the mvue of b under the restriction $\Psi b = 0$,

$R_{\Psi_0}^2$ is the squared multiple correlation under the restriction $\Psi_0 b = 0$, and

R_{Ψ}^2 is the squared multiple correlation under the restriction

$\Psi b = 0$.

The Chipman and Rao computational form for F is different from the form in (7), but the two are equivalent. (See Rao, 1965, pp. 199-200).

MVUE for a Criterion Cluster

The restriction $\alpha_1 = \alpha_2 = \dots = \alpha_t$ and $b_1 = b_2 = \dots = b_t$ can be expressed in the form $\Psi b = 0$ as

$$(8) \quad (t-1)(p+1) \quad \left\{ \begin{array}{c} \left[\begin{array}{cccccc} I & -I & 0 & \dots & & \\ & & -I & 0 & \dots & \\ & & & \ddots & & \\ & 0 & & & & 0 \\ & & & & 0 & \\ & & & & & \\ I & 0 & \dots & 0 & -I & 0 & \dots & 0 \end{array} \right] \begin{array}{c} \alpha_1 \\ b_1 \\ \\ \alpha_k \\ b_k \end{array} \end{array} \right\} = 0$$

$\underbrace{\hspace{10em}}_{t(p+1)} \quad \underbrace{\hspace{10em}}_{(k-t)(p+1)}$

where I is the $(p+1) \times (p+1)$ identity matrix. To express model (1b) in a form similar to equation (5) under the above restriction (8), the $k(p+1) \times (k-t+1)(p+1)$ matrix B , where

$$B' = \left[\begin{array}{c|c} \overbrace{I \dots I}^{t(p+1)} & \overbrace{0 \dots 0}^{(k-t)(p+1)} \\ \hline 0 \dots 0 & I \\ & \ddots & 0 \\ & 0 & \ddots & I \end{array} \right] \left. \vphantom{\begin{array}{c|c} \overbrace{I \dots I}^{t(p+1)} & \overbrace{0 \dots 0}^{(k-t)(p+1)} \end{array}} \right\} (k-t+1)(p+1)$$

and the $(k-t+1)(p+1)$ vector of new parameters θ , where

$$\theta' = [\alpha_\Psi \ b_\Psi \ \alpha_{t+1} \ b_{t+1} \ \dots \ \alpha_k \ b_k],$$

is introduced into (1b) to yield the model

$$(9) \quad E(Y|X) = \begin{bmatrix} u_1 X_1 \\ \vdots \\ u_t X_t \\ \vdots \\ u_{t+1} X_{t+1} \\ \vdots \\ 0 \end{bmatrix} \begin{bmatrix} 0 \\ \vdots \\ 0 \end{bmatrix} \begin{bmatrix} \alpha_\Psi \\ b_\Psi \\ \alpha_{t+1} \\ b_{t+1} \\ \vdots \\ \alpha_k \\ b_k \end{bmatrix} \quad \text{with } D(Y|X) = \sigma^2 I.$$

The effect of B is to pool the observations for criteria 1, ..., t. The mvue $\hat{\alpha}_\Psi$ and \hat{b}_Ψ , for the criterion cluster (1, 2, ..., t) formed from criteria 1, ..., t can be calculated in either of two ways: pool the observations as in (9) and compute $\hat{\alpha}_\Psi$ and \hat{b}_Ψ from the normal equations

$$(9a) \quad \left\{ \begin{bmatrix} n_1 & u_1' X_1 \\ X_1' u_1 & X_1' X_1 \end{bmatrix} + \dots + \begin{bmatrix} n_t & u_t' X_t \\ X_t' u_t & X_t' X_t \end{bmatrix} \right\} \begin{bmatrix} \hat{\alpha}_\Psi \\ \hat{b}_\Psi \end{bmatrix} = \left\{ \begin{bmatrix} u_1' y_1 \\ X_1' y_1 \end{bmatrix} + \dots + \begin{bmatrix} u_t' y_t \\ X_t' y_t \end{bmatrix} \right\}$$

or if the predictor sums-of-squares and cross-product matrices are proportional, i.e.,

$$(9b) \quad \frac{1}{n_1} \begin{bmatrix} n_1 & u_1' X_1 \\ X_1' u_1 & X_1' X_1 \end{bmatrix} = \frac{1}{n_2} \begin{bmatrix} n_2 & u_2' X_2 \\ X_2' u_2 & X_2' X_2 \end{bmatrix} = \dots = \frac{1}{n_t} \begin{bmatrix} n_t & u_t' X_t \\ X_t' u_t & X_t' X_t \end{bmatrix},$$

then $\hat{\alpha}_\Psi$ and \hat{b}_Ψ can be calculated from $\hat{\alpha}_1, \hat{b}_1, \dots, \hat{\alpha}_t, \hat{b}_t$ given in (2) without forming the sum of matrices on the left hand side in (9a). Using (9b) this sum of matrices is

$$(9c) \quad \left\{ \begin{bmatrix} n_1 & u_1' X_1 \\ X_1' u_1 & X_1' X_1 \end{bmatrix} + \dots + \begin{bmatrix} n_t & u_t' X_t \\ X_t' u_t & X_t' X_t \end{bmatrix} \right\} = \frac{N_t}{n_1} \begin{bmatrix} n_1 & u_1' X_1 \\ X_1' u_1 & X_1' X_1 \end{bmatrix} \quad \text{for } i = 1, \dots, t$$

where $N_t = n_1 + n_2 + \dots + n_t$. Using (9c) the solution of (9a) is

$$\begin{aligned} \begin{bmatrix} \hat{\alpha}_\Psi \\ \hat{b}_\Psi \end{bmatrix} &= \sum_{i=1}^t \left(\begin{bmatrix} n_i u_i' X_i \\ X_i' u_i X_i' X_i \end{bmatrix} + \dots + \begin{bmatrix} n_t u_t' X_t \\ X_t' u_t X_t' X_t \end{bmatrix} \right)^{-1} \begin{bmatrix} u_i' y_i \\ X_i' y_i \end{bmatrix} \\ &= \sum_{i=1}^t \frac{n_i}{N_t} \begin{bmatrix} n_i u_i' X_i \\ X_i' u_i X_i' X_i \end{bmatrix}^{-1} \begin{bmatrix} u_i' y_i \\ X_i' y_i \end{bmatrix} \end{aligned}$$

Thus, the mvue for a criterion cluster are

$$(10) \quad \begin{bmatrix} \hat{\alpha}_\Psi \\ \hat{b}_\Psi \end{bmatrix} = \frac{n_1}{N_t} \begin{bmatrix} \hat{\alpha}_1 \\ \hat{b}_1 \end{bmatrix} + \dots + \frac{n_t}{N_t} \begin{bmatrix} \hat{\alpha}_t \\ \hat{b}_t \end{bmatrix}$$

When (9b) holds, the formula for the standardized regression weights for a criterion cluster is easy to obtain. Let $\hat{\beta}_\Psi, \hat{\beta}_1, \dots, \hat{\beta}_t$ be the standardized weights corresponding to the raw weights $\hat{b}_\Psi, \hat{b}_1, \dots, \hat{b}_t$; let Q_i be the $p \times p$ diagonal matrix with its elements equal to the standard deviations calculated from the observation matrix X_i for the p independent variables; let Q_Ψ be the $p \times p$ diagonal matrix with its elements equal to the standard deviations calculated from the pooled observation matrix $[X_1' X_2' \dots X_t']'$ for the p independent variables; and let $\sigma_\Psi^2, \sigma_1^2, \dots, \sigma_t^2$ be the sample variances for the vectors of criterion observations $[y_1' y_2' \dots y_t']', y_1, \dots, y_t$, respectively. By definition the standardized weights are

$$\hat{\beta}_\Psi = \frac{Q_\Psi \hat{b}_\Psi}{\sigma_\Psi}, \quad \hat{\beta}_1 = \frac{Q_1 \hat{b}_1}{\sigma_1}, \quad \dots, \quad \hat{\beta}_t = \frac{Q_t \hat{b}_t}{\sigma_t}.$$

From (9b), $Q_\Psi = Q_1 = \dots = Q_t$; therefore using (10), the formula for the standardized weights for a criterion cluster is

$$(10a) \quad \hat{\beta}_\Psi = \frac{1}{N_t \sigma_\Psi} (n_1 \sigma_1 \hat{\beta}_1 + \dots + n_t \sigma_t \hat{\beta}_t).$$

Multiple Correlation Coefficient for a Criterion Cluster

Let $R_\Psi^2, R_1^2, \dots, R_t^2$ be the squared multiple correlation coefficients for the criterion cluster formed from criteria 1, \dots , t and for the t criteria y_1, \dots, y_t , respectively; let c_i be the $p \times 1$ vector of intercorrelations calculated from the observations X_i and y_i between the p independent variables and the i -th criterion; and let c_Ψ be the $p \times 1$ vector of intercorrelations calculated from the pooled observations $[X_1' X_2' \dots X_t']'$ and $[y_1' y_2' \dots y_t']'$ between the p independent variables and the criterion cluster (1, 2, \dots , t). By definition,

$$\begin{aligned} n_i \sigma_i Q_i c_i &= X_i' y_i - \frac{1}{n_i} X_i' u_i u_i' y_i \quad \text{for } i=1, \dots, k \text{ and} \\ N_t \sigma_\Psi Q_\Psi c_\Psi &= (X_1' y_1 + \dots + X_t' y_t) - \frac{1}{N_t} [X_1' u_1 + \dots + X_t' u_t] [u_1' y_1 + \dots + u_t' y_t]. \end{aligned}$$

From (9c), $\frac{1}{N_t} [X_1' u_1 + \dots + X_t' u_t] = \frac{1}{n_i} X_i' u_i$ for $i=1, \dots, t$. Therefore,

$$N_t \sigma_\Psi Q_\Psi c_\Psi = n_1 \sigma_1 Q_1 c_1 + \dots + n_t \sigma_t Q_t c_t.$$

But $Q_\Psi = Q_1 = \dots = Q_t$ so the validity coefficients for a criterion cluster are

$$(10b) c_{\Psi} = \frac{1}{N_t \sigma_{\Psi}} (n_1 \sigma_1 c_1 + \dots + n_t \sigma_t c_t).$$

The squared multiple correlation coefficient for the cluster

(1, 2, ..., t) is

$$(10c) R_{\Psi}^2 = \hat{\beta}_{\Psi} c_{\Psi} = \frac{1}{N_t \sigma_{\Psi}^2} (n_1 \sigma_1 \hat{\beta}_1 + \dots + n_t \sigma_t \hat{\beta}_t)' (n_1 \sigma_1 c_1 + \dots + n_t \sigma_t c_t).$$

Hypothesis Testing

The critical region given in (7) for the hypothesis (6) requires the calculation of the error sum of squares or the squared multiple correlation coefficient for model (1b) when restrictions are imposed on the unknown parameters. The error sum of squares, ESS, for model (1b) when there are no restrictions on the unknown parameters is equal to the sum of the error sum of squares, ESS_i, for the k models (see (3)), i.e.,

$$ESS = ESS_1 + ESS_2 + \dots + ESS_k.$$

Let m_0 and σ_0^2 be the criterion mean and variance calculated from the pooled criterion observation vector Y, and let m_1, \dots, m_k be the criterion means for y_1, \dots, y_k , respectively. Then

$$ESS_i = n_i \sigma_i^2 (1 - R_i^2) \quad \text{for } i=1, \dots, k$$

$$Nm_0 = n_1 m_1 + n_2 m_2 + \dots + n_k m_k$$

$$N\sigma_0^2 = n_1 (\sigma_1^2 + m_1^2) + \dots + n_k (\sigma_k^2 + m_k^2) - Nm_0^2$$

Therefore the squared multiple correlation, R^2 , for (1b) is

$$(11) \quad R^2 = \frac{N\sigma_0^2 - ESS}{N\sigma_0^2} = \frac{n_1 (\sigma_1^2 R_1^2 + m_1^2) + \dots + n_k (\sigma_k^2 R_k^2 + m_k^2) - Nm_0^2}{n_1 (\sigma_1^2 + m_1^2) + \dots + n_k (\sigma_k^2 + m_k^2) - Nm_0^2}$$

The error sum of squares, ESSH, for (9) is

$$ESSH = ESS_{\Psi} + ESS_{t+1} + \dots + ESS_k$$

where $ESS_{\Psi} = N_t \sigma_{\Psi}^2 (1 - R_{\Psi}^2)$. Therefore the squared multiple correlation, R_0^2 , for (9) is

$$R_0^2 = \frac{N\sigma_0^2 - ESSH}{N\sigma_0^2}$$

The hypothesis (8) can be tested at the α significance level by computing

$$(11a) \quad F = \left(\frac{N-k(p+1)}{(t-1)(p+1)} \right) \left(\frac{R^2 - R_0^2}{1 - R^2} \right)$$

and rejecting (8) if F exceeds the $100(1-\alpha)\%$ point of the central F distribution with $(t-1)(p+1)$ and $N - k(p+1)$ degrees of freedom.

Application to a Four Criteria Model; A Worked Example

Given four criteria y_1, y_2, y_3 , and y_4 , where y_i is an $n_i \times 1$ vector of observations, and the predictor matrices X_1, X_2, X_3 , and X_4 , where X_i is an $n_i \times p$ matrix of observations on p independent variables, the

greatest predictive power is attained when each criterion variable is predicted from its regression on the independent variables. The initial stage, i.e., Stage 4, employs the following model:

$$(12) E \begin{bmatrix} y_1 \\ y_2 \\ y_3 \\ y_4 \end{bmatrix} = \begin{bmatrix} u_1 X_1 & 0 & 0 & 0 \\ 0 & u_2 X_2 & 0 & 0 \\ 0 & 0 & u_3 X_3 & 0 \\ 0 & 0 & 0 & u_4 X_4 \end{bmatrix} \begin{bmatrix} \alpha_1 \\ b_1 \\ \alpha_2 \\ b_2 \\ \alpha_3 \\ b_3 \\ \alpha_4 \\ b_4 \end{bmatrix} = \begin{bmatrix} \alpha_1 u_1 + b_1 X_1 \\ \alpha_2 u_2 + b_2 X_2 \\ \alpha_3 u_3 + b_3 X_3 \\ \alpha_4 u_4 + b_4 X_4 \end{bmatrix} \text{ with } D \begin{bmatrix} y_1 \\ y_2 \\ y_3 \\ y_4 \end{bmatrix} = \sigma^2 I.$$

$4 \times 4 \quad \quad \quad 4 \times 1 \quad \quad \quad 4 \times 1$

The mvue $\hat{\alpha}_i$ and \hat{b}_i , for α_i and b_i are obtained from (2) and the squared multiple correlation coefficient, ${}_4 R^2$, for model (12) is obtained from (11).

For Stage 3, assume (9b) holds for X_1, X_2, X_3 , and X_4 . Under the linear hypothesis $\alpha_1 = \alpha_2$ and $b_1 = b_2$, the mvue $\hat{\alpha}_{12}$ and \hat{b}_{12} , for the criterion cluster (1,2) formed from criteria 1 and 2 are (see (10))

$$\begin{bmatrix} \hat{\alpha}_{12} \\ \hat{b}_{12} \end{bmatrix} = \frac{n_1}{(n_1 + n_2)} \begin{bmatrix} \hat{\alpha}_1 \\ \hat{b}_1 \end{bmatrix} + \frac{n_2}{n_1 + n_2} \begin{bmatrix} \hat{\alpha}_2 \\ \hat{b}_2 \end{bmatrix}$$

The standard weights, $\hat{\beta}_{12}$, and the validities, c_{12} , for the cluster (1,2) are (see (10a) and (10b))

$$\begin{aligned} \hat{\beta}_{12} &= \frac{1}{(n_1 + n_2)\sigma_{12}} (n_1 \sigma_1 \hat{\beta}_1 + n_2 \sigma_2 \hat{\beta}_2), \text{ and} \\ c_{12} &= \frac{1}{(n_1 + n_2)\sigma_{12}} (n_1 \sigma_1 c_1 + n_2 \sigma_2 c_2), \text{ where} \\ (n_1 + n_2)\sigma_{12}^2 &= n_1(\sigma_1^2 + m_1^2) + n_2(\sigma_2^2 + m_2^2) - \frac{(n_1 m_1 + n_2 m_2)^2}{n_1 + n_2}. \end{aligned}$$

The model used to obtain these estimates is (see (9))

$$(13) E \begin{bmatrix} y_1 \\ y_2 \\ y_3 \\ y_4 \end{bmatrix} = \begin{bmatrix} u_1 X_1 & 0 & 0 \\ u_2 X_2 & 0 & 0 \\ 0 & u_3 X_3 & 0 \\ 0 & 0 & u_4 X_4 \end{bmatrix} \begin{bmatrix} \alpha_{12} \\ b_{12} \\ \alpha_3 \\ b_3 \\ \alpha_4 \\ b_4 \end{bmatrix} = \begin{bmatrix} \alpha_{12} \begin{bmatrix} u_1 \\ u_2 \end{bmatrix} + b_{12} \begin{bmatrix} X_1 \\ X_2 \end{bmatrix} \\ \alpha_3 u_3 + b_3 X_3 \\ \alpha_4 u_4 + b_4 X_4 \end{bmatrix} \text{ with } D \begin{bmatrix} y_1 \\ y_2 \\ y_3 \\ y_4 \end{bmatrix} = \sigma^2 I.$$

The squared multiple correlation coefficient, ${}_3 R^2$, for (13) is (from (11) with $k=3$)

$$\begin{aligned} {}_3 R^2 &= \frac{[(n_1 + n_2)(\sigma_{12}^2 R_{12}^2 + m_{12}^2) + n_3(\sigma_3^2 R_3^2 + m_3^2) + n_4(\sigma_4^2 R_4^2 + m_4^2) - N m_0^2]}{[(n_1 + n_2)(\sigma_{12}^2 + m_{12}^2) + n_3(\sigma_3^2 + m_3^2) + n_4(\sigma_4^2 + m_4^2) - N m_0^2]}, \text{ where} \\ R_{12}^2 &= \hat{\beta}_{12} c_{12}, \quad m_{12} = \frac{(n_1 m_1 + n_2 m_2)}{(n_1 + n_2)}, \quad N = n_1 + n_2 + n_3 + n_4, \text{ and} \end{aligned}$$

$$N m_0 = n_1 m_1 + n_2 m_2 + n_3 m_3 + n_4 m_4.$$

(11a) can now be used to test at the α significance level the hypothesis $H1: \alpha_1 = \alpha_2$ and $b_1 = b_2$ by computing

$$F = \left(\frac{N-4(p+1)}{(p+1)} \right) \left(\frac{{}_4R^2 - {}_3R^2}{(1-{}_4R^2)} \right)$$

and rejecting $H1$ if F exceeds $F_{\alpha}(p+1, N-4(p+1))$.

For Stage 2, accepting $H1$ as true, the additional restrictions $\alpha_3 = \alpha_4$ and $b_3 = b_4$ are imposed and the mvue, $\hat{\alpha}_{34}$ and \hat{b}_{34} , for the criterion cluster (3,4) formed from criteria 3 and 4 are

$$\begin{bmatrix} \hat{\alpha}_{34} \\ \hat{b}_{34} \end{bmatrix} = \frac{n_3}{n_3 + n_4} \begin{bmatrix} \hat{\alpha}_3 \\ \hat{b}_3 \end{bmatrix} + \frac{n_4}{n_3 + n_4} \begin{bmatrix} \hat{\alpha}_4 \\ \hat{b}_4 \end{bmatrix}$$

The standard weights, $\hat{\beta}_{34}$, and the validities, c_{34} , for the cluster (3,4) are

$$\hat{\beta}_{34} = \frac{1}{(n_3 + n_4)\sigma_{34}} (n_3\sigma_3\hat{\beta}_3 + n_4\sigma_4\hat{\beta}_4), \text{ and}$$

$$c_{34} = \frac{1}{(n_3 + n_4)\sigma_{34}} (n_3\sigma_3c_3 + n_4\sigma_4c_4), \text{ where}$$

$$(n_3 + n_4)\sigma_{34}^2 = n_3(\sigma_3^2 + m_3^2) + n_4(\sigma_4^2 + m_4^2) - \frac{(n_3m_3 + n_4m_4)^2}{(n_3 + n_4)}$$

The model used to obtain these estimates is

$$(14) E \begin{bmatrix} y_1 \\ y_2 \\ y_3 \\ y_4 \end{bmatrix} = \begin{bmatrix} u_1X_1 & 0 \\ u_2X_2 & 0 \\ 0 & u_3X_3 \\ & u_4X_4 \end{bmatrix} \begin{bmatrix} \alpha_{12} \\ b_{12} \\ \alpha_{34} \\ b_{34} \end{bmatrix} = \begin{bmatrix} \alpha_{12} & \begin{bmatrix} u_1 \\ u_2 \end{bmatrix} \\ \alpha_{34} & \begin{bmatrix} u_3 \\ u_4 \end{bmatrix} \end{bmatrix} \begin{bmatrix} X_1 \\ X_2 \\ X_3 \\ X_4 \end{bmatrix} + \begin{bmatrix} b_{12} \\ b_{34} \end{bmatrix} \text{ with } D \begin{bmatrix} y_1 \\ y_2 \\ y_3 \\ y_4 \end{bmatrix} = \sigma^2 I.$$

The squared multiple correlation coefficient, ${}_2R^2$, for (14) is (from (11) with $k=2$)

$${}_2R^2 = \frac{[(n_1 + n_2)(\sigma_{12}^2 R_{12}^2 + m_{12}^2) + (n_3 + n_4)(\sigma_{34}^2 R_{34}^2 + m_{34}^2) - Nm_0^2]}{[(n_1 + n_2)(\sigma_{12}^2 + m_{12}^2) + (n_3 + n_4)(\sigma_{34}^2 + m_{34}^2) - Nm_0^2]}$$

where $R_{34}^2 = \hat{\beta}_{34}c_{34}$, $(n_3 + n_4)m_{34} = n_3m_3 + n_4m_4$. Equation (11a) can now be used to test at the α significance level the hypothesis

$H2: \alpha_3 = \alpha_4$ and $b_3 = b_4$ given $H1$ is true by computing

$$F = \left(\frac{N-3(p+1)}{(p+1)} \right) \left(\frac{{}_3R^2 - {}_2R^2}{(1-{}_3R^2)} \right)$$

and rejecting $H2$ if F exceeds $F_{\alpha}(p+1, N-3(p+1))$.

Equation (11a) can also be used to test the hypothesis

$H3: \alpha_1 = \alpha_2, b_1 = b_2, \alpha_3 = \alpha_4, \text{ and } b_3 = b_4$ by computing

$$F = \left(\frac{N-4(p+1)}{2(p+1)} \right) \left(\frac{{}_4R^2 - {}_2R^2}{(1-{}_4R^2)} \right)$$

and rejecting H3 if F exceeds $F_{\alpha}(2(p+1), N-4(p+1))$.

For Stage 1, accepting H2 as true, the additional restrictions $\alpha_{12} = \alpha_{34}$ and $b_{12} = b_{34}$ are imposed and the mvue, $\hat{\alpha}_{1234}$ and \hat{b}_{1234} , for the criterion cluster (1,2,3,4) formed from all four criteria are

$$\begin{bmatrix} \hat{\alpha}_{1234} \\ \hat{b}_{1234} \end{bmatrix} = \frac{(n_1+n_2)}{N} \begin{bmatrix} \hat{\alpha}_{12} \\ \hat{b}_{12} \end{bmatrix} + \frac{(n_3+n_4)}{N} \begin{bmatrix} \hat{\alpha}_{34} \\ \hat{b}_{34} \end{bmatrix}$$

The standard weights, $\hat{\beta}_{1234}$, and the validities, c_{1234} , for the cluster (1,2,3,4) are

$$\hat{\beta}_{1234} = \frac{1}{N\sigma_{1234}} (n_1+n_2)\sigma_{12}\hat{\beta}_{12} + (n_3+n_4)\sigma_{34}\hat{\beta}_{34}, \text{ and}$$

$$c_{1234} = \frac{1}{N\sigma_{1234}} (n_1+n_2)\sigma_{12}c_{12} + (n_3+n_4)\sigma_{34}c_{34}, \text{ where}$$

$$N\sigma_{1234}^2 = (n_1+n_3)(\sigma_{12}^2 + m_{12}^2) + (n_3+n_4)(\sigma_{34}^2 + m_{34}^2) - Nm_{1234}^2, \text{ and}$$

$$Nm_{1234} = n_1m_1 + n_2m_2 + n_3m_3 + n_4m_4.$$

The model used to obtain the estimates for cluster (1,2,3,4) is

$$(15) E \begin{bmatrix} y_1 \\ y_2 \\ y_3 \\ y_4 \end{bmatrix} = \begin{bmatrix} u_1 X_1 \\ u_2 X_2 \\ u_3 X_3 \\ u_4 X_4 \end{bmatrix} \begin{bmatrix} \alpha_{1234} \\ b_{1234} \end{bmatrix} + b_{1234} \begin{bmatrix} X_1 \\ X_2 \\ X_3 \\ X_4 \end{bmatrix} \text{ with } D \begin{bmatrix} y_1 \\ y_2 \\ y_3 \\ y_4 \end{bmatrix} = \sigma^2 I.$$

The squared multiple correlation coefficient, ${}_1R^2$, for (15) is

$${}_1R^2 = \hat{\beta}_{1234} c_{1234}.$$

Equation (11a) can now be used to test at the α significance level the hypothesis

H4: $\alpha_{12} = \alpha_{34}$ and $b_{12} = b_{34}$, given $\alpha_1 = \alpha_2$, $\alpha_3 = \alpha_4$, $b_1 = b_2$ and $b_3 = b_4$ by computing

$$F = \left(\frac{N-2(p+1)}{(p+1)} \right) \left(\frac{{}_2R^2 - {}_1R^2}{(1-{}_2R^2)} \right)$$

and rejecting H4 if F exceeds $F_{\alpha}(p+1, N-2(p+1))$. The hypothesis

H5: $\alpha_1 = \alpha_2 = \alpha_3 = \alpha_4$ and $b_1 = b_2 = b_3 = b_4$

can be tested at the α significance level by computing

$$F = \left(\frac{N-4(p+1)}{3(p+1)} \right) \left(\frac{{}_4R^2 - {}_1R^2}{(1-{}_4R^2)} \right)$$

and rejecting H5 if F exceeds $F_{\alpha}(3(p+1), N-4(p+1))$.

APPENDIX C: HIER-GRP SAMPLE OUTPUT

The HIER-GRP sample output provided in this appendix was produced by using the Univac 1108 runstream which precedes it. The sample analysis involves a grouping problem with nine regression equations having nine predictors.

UNIVAC 1108 RUNSTREAM FOR HIER-GRP SAMPLE PROBLEM

BRUN T478.3659.T
MAXI T=I.HIER-GRP

009009620

SAMPLE HIERARCHICAL GROUPING ANALYSIS FOR A PROBLEM WITH NINE
REGRESSION EQUATIONS CONTAINING NINE PREDICTOR VARIABLES
(11F7.0)

498.	498.	498.	498.	498.	498.	498.	498.	498.
(LF12.6)								
56.451007	21.308644							
53.395582	21.914342							
68.744980	16.605052							
72.044176	18.446208							
60.863453	17.790080							
52.500000	15.220105							
53.965863	15.463798							
61.050200	18.499403							
59.132530	14.158818							
(LF12.6/3F12.6)								
.210613	.084266	.690537	.044687	.022704	.019188			
.030065	.051014	.002266						
.497278	.253267	.146937	.111735	-.048070	.070620			
.023948	.067965	.002673						
.830726	.062409	.110464	.066591	-.017240	.013254			
.008630	-.008133	.001335						
.000000	.503307	.046976	.400246	-.098074	.081784			
.088532	.010101	.055075						
.501937	.228462	.241215	.079214	-.058422	.015964			
.027251	.071612	.017675						
.157068	.523549	.177268	.109043	-.119310	.033768			
.061973	.125317	.077995						
.625357	.140070	.179064	.078076	-.055456	.063479			
.007705	.036213	.039056						
.054018	.009892	-.032781	.111520	-.159781	.119546			
.065051	.132338	.072512						
.183373	.264566	.198929	.281333	-.088878	.067113			
.030136	.106099	.041553						
(LF12.6/3F12.6)								
.851747	.403108	.943397	.330665	-.267945	.263114			
.260275	.748397	.061240						
.812347	.525137	.748172	.400812	-.306481	.277655			
.284223	.641246	.048847						
.963222	.380671	.830779	.326702	-.325629	.318978			
.230869	.666403	.082854						
.379912	.716074	.383850	.652332	-.200817	.054977			
.400267	.345576	.065272						
.867424	.523468	.823604	.368907	-.337009	.251625			
.294623	.694826	.074963						
.641551	.734258	.649314	.466729	-.317681	.130361			
.383839	.589730	.095018						
.902620	.431595	.817043	.351056	-.347421	.323654			
.243765	.672775	.103907						
.442066	.726975	.420952	.427142	-.284123	.129945			
.355847	.429272	.062678						
.627808	.539934	.635186	.526863	-.292518	.184302			
.296842	.565390	.073218						
(5X, 2F18.4)								
1	1025.3594	160.2755						
2	281.0361	50.0347						
3	43.6386	30.6446						
4	2.9217	.8665						
5	.6526	.4761						
6	3.9398	1.3035						
7	343.2791	44.7462						
8	40.7771	30.2306						
9	.7048	.4561						

END

COMPUTATIONAL SCIENCES DIVISION
AF HUMAN RESOURCES LABORATORY
AIR FORCE SYSTEMS COMMAND

HIERARCHICAL GROUPING PROGRAM HIER-GRP

VERSION DATE 11 JAN 1978

I. CONTROL CARD PARAMETERS

NUMBER OF REGRESSION EQUATIONS = 9 NUMBER OF PREDICTOR VARIABLES = 9
GROUPING OPTION = 6 NUMBER OF HEADER CARDS = 2

PROBLEM HEADER LABEL

SAMPLE HIERARCHICAL GROUPING ANALYSIS FOR A PROBLEM WITH NINE
REGRESSION EQUATIONS CONTAINING NINE PREDICTOR VARIABLES

II. FORMAT CARDS AND INPUT DATA

FORMAT TO READ SM(1) = (11F7.0)

FORMAT TO READ SM(1) AND SSD(1) = (2F12.6)

EQUATION	N	CRITERION MEAN	CRITERION SD
1	498.	56.45181	21.30664
2	498.	63.39558	21.91434
3	498.	68.74498	16.60505
4	498.	72.04418	18.44621
5	498.	60.86345	17.79008
6	498.	52.50000	15.22011
7	498.	53.95536	15.46380
8	498.	61.05020	18.49940
9	498.	59.13253	14.15082

FORMAT TO READ BETA WEIGHTS = (6F12.6/3F12.6)

BETA WEIGHTS	1	2	3	4	5	6	7	8	9
EQ 1	.2106	.0843	.6905	.0447	.0227	.0192	.0301	.0510	.0023
EQ 2	.4973	.2533	.1469	.1117	-.0481	.0706	.0239	.0680	.0027
EQ 3	.8307	.0624	.1105	.0666	-.0172	.0133	.0086	-.0081	.0013
EQ 4	.0000	.5033	.0470	.4002	-.0981	.0818	.0885	.0101	.0551
EQ 5	.5019	.2285	.2412	.0792	-.0584	.0160	.0273	.0716	.0177
EQ 6	.1570	.5235	.1773	.1390	-.1193	.0338	.0620	.1253	.0780
EQ 7	.6254	.1401	.1791	.0781	-.0555	.0635	.0079	.0362	.0391
EQ 8	.0546	.6099	-.0328	.1115	-.1598	.1195	.0659	.1323	.0725
EQ 9	.1834	.2646	.1989	.2813	-.0889	.0671	.0301	.1061	.0416

FORMAT TO READ VALIDITIES = (6F12.6/3F12.6)

VALIDITIES	1	2	3	4	5	6	7	8	9
EQ 1	.8517	.4031	.9434	.3307	-.2679	.2631	.2603	.7484	.0612
EQ 2	.8123	.5251	.7482	.4008	-.3065	.2777	.2842	.6412	.0488

EQU 3	.9632	.3807	.4308	.3267	.3256	.3190	.2309	.6664	.0829
EQU 4	.3799	.7181	.3439	.6523	.2008	.0550	.4003	.3456	.0653
EQU 5	.4674	.5235	.6236	.3889	.3370	.2516	.2948	.6948	.0750
EQU 6	.6416	.7343	.6493	.4667	.3177	.1304	.3838	.5897	.0950
EQU 7	.9026	.4316	.8170	.3511	.3474	.3237	.2438	.6728	.1039
EQU 8	.4421	.7270	.4210	.4271	.2841	.1299	.3558	.4293	.0627
EQU 9	.6278	.5399	.6352	.5269	.2925	.1843	.2988	.5654	.0732

FORMAT TO HEAD PM(L) AND PS(L) = (5X,2F18.4)

PREDICTOR	PREDICTOR MEAN	PREDICTOR SD
1	1025.35941	160.27550
2	231.03610	50.03470
3	43.63860	30.64460
4	2.92170	.86650
5	.55260	.47610
6	3.93940	1.30350
7	393.27910	44.74820
8	40.77710	30.23260
9	.70480	.45610

III. HIERARCHICAL GROUPING RESULTS

MINIMIZED DECISION VALUE = ORU(KU+1)-ORU(KU)
 ORU(KU) = R SQUARED FOR KU SYSTEMS.
 KU = NUMBER OF SYSTEMS REMAINING AT KU STAGE.

GROUPING OPTION 6

9 INITIAL SYSTEMS RSQ = .8230									
SYS	RSQ	SYS	RSQ	SYS	RSQ	SYS	RSQ	SYS	RSQ
1	.9247	2	.7765	3	.9140	4	.7072	5	.8673
6	.7986	7	.8688	8	.6472	9	.6430		
STAGE = 3 OVERALL RSQ = .8203									

F-TEST FOR THE EQUALITY OF REGRESSION PARAMETERS

GROUPING THIS STAGE										FOR SYS'S COMBINED UP TO THIS STAGE									
SYSTEMS										SYSTEMS									
CHANGE FROM										CHANGE FROM									
SYS	NO.	RSQ	RSQ	RSQ	RSQ	RSQ	RSQ	RSQ	RSQ	SYS	NO.	RSQ	RSQ	RSQ	RSQ	RSQ	RSQ	RSQ	RSQ
IDENT MEMBERS	CASES	RSQ	RSQ	RSQ	RSQ	RSQ	RSQ	RSQ	RSQ	IDENT MEMBERS	CASES	RSQ	RSQ	RSQ	RSQ	RSQ	RSQ	RSQ	RSQ
2	1	.498	.7765	.498	.7765	.498	.7765	.498	.7765	9	9	.0026	.0026	.0026	.0026	.0026	.0026	.0026	.0026
5	1	.498	.8673	.498	.8673	.498	.8673	.498	.8673	10	10	.4392	.4392	.4392	.4392	.4392	.4392	.4392	.4392
DECISION VALUE = .0026										FSTAT = 6.53 SIG LVL = .0000									
FSTAT = .0026										FSTAT = 6.53 SIG LVL = .0000									

SYSTEMS SUMMARY ROSTER

STAGE	SYS	NO.	RSQ	RSQ	RSQ	RSQ	RSQ	RSQ	RSQ
IDENT LOSS MEMBERS	CASES	RSQ	RSQ	RSQ	RSQ	RSQ	RSQ	RSQ	RSQ
8	.0026	2	.8028	.996	2	5			
BETA WEIGHTS FOR THE NEW SYSTEM 2									
NEW SYS CRITERION MEAN = 62.1295									
NEW SYS CRITERION SD = 19.9991									

COMPUTER OUTPUT FROM HIER-GHP SAMPLE PROBLEM

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[illegible]

7 SINGLE MEMBER SYSTEMS									
	1	3	4	6	7	8	9		
STAGE = 7 OVERALL RSQ = .8117									
F-TEST FOR THE EQUALITY OF REGRESSION PARAMETERS									
SYSTEMS									
GROUPING THIS STAGE									
FOR SYS'S COMBINED AT THIS STAGE									
FOR SYS'S COMBINED UP TO THIS STAGE									
SYS NO.	NO.		CHANGE FROM		CHANGE FROM				
IDENT MEMBERS	CASES	RSQ	8 SYSTEMS		9 SYSTEMS		RESIDUAL		
8	1	.498	.6472	RSQ	.0086	.1797	.0112	.1770	
9	1	.498	.6430	DF	10	4402	20	4392	
DECISION VALUE =		.0086		FSTAT =		21.10		SIG LVL = .0000	
				FSTAT =		13.95		SIG LVL = .0000	

SYSTEM45 SUMMARY ROSTER									
STAGE	SYS	NO.	NO.	SYS					
IDENT	LOSS	MEMBERS	MSQ	CASES	IDENT	IDENTIFICATION OF OTHER MEMBERS			
8	.J026	2	.8028	996	2	5			
7	.0086	2	.5960	996	8	9			
•									
					BETA WEIGHTS FOR THE NEW SYSTEM				
					8				

					1	2	3	4	5
					.1094	.4554	.0670	.1832	-.1277
					•				
					NEW SYS CRITERION MEAN = 60.0914				
					NEW SYS CRITERION SD = 16.5006				
					6				
					7				
					.0958				
					.1197				
					.0585				
•									
					RAW SCORE WEIGHTS FOR THE NEW SYSTEM				
					8				

					1	2	3	4	5
					.0113	.1502	.0361	.3.4890	-4.4258
					1.2128				
					.0184				
					.0653				
					2.1155				
					REGRESSION CONSTANT = -17.7861				

5 SINGLE MEMBER SYSTEMS												1	3	4	6	7				
STAGE = 6												OVERALL R ² = .1023								
F-TTEST FOR THE EQUALITY OF REGRESSION PARAMETERS																				
SYSTEMS																				
GROUPING THIS STAGE												FOR SYS'S COMBINED AT THIS STAGE			FOR SYS'S COMBINED UP TO THIS STAGE					
SYS												NO.			CHANGE FROM			CHANGE FROM		
IDENT MEMBERS												CASES			R ²			RESIDUAL		
6												1			.498 .7966			.1770		
7												1			.454 .8668			.0206		
															DF			DF		
															10			30		
															4412			4392		
DECISION VALUE =												.0094			FSTAT =			17.06 SIG LVL = .0000		

	STAGE	SYS NO.	SYS
SYSTEMS SUMMARY ROSTER			

IDENT LOSS MEMBERS		RSQ	CASES	IDENT	IDENTIFICATION OF OTHER MEMBERS	
8	.0026	2	.8026	996	2	5
6	.0094	2	.7707	996	6	7

BETA WEIGHTS FOR THE NEW SYSTEM				6	REGRESSION CONSTANT = -30.0948				
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STAGE = 5										OVERALL RSQ = .7385										F-TEST FOR THE EQUALITY OF REGRESSION PARAMETERS																													
SYSTEMS										GROUPING THIS STAGE										FOR SYS'S COMBINED AT THIS STAGE										FOR SYS'S COMBINED UP TO THIS STAGE																			
SYS										NO.										NO.										CHANGE FROM																			
IDENT MEMBERS										CASES										RSQ										RSQ										CHANGE FROM									
A SYSTEMS										A SYSTEMS										A SYSTEMS										A SYSTEMS										CHANGE FROM									
RESIDUAL										RESIDUAL										RESIDUAL										RESIDUAL										CHANGE FROM									

SYSTEMS SUMMARY RUSTER									

DECISION VALUE =									
2	2	996 .8026	•	RSQ	•	.0138	•	.1977	•
3	1	498 .9440	•	DF	•	10	•	4422	•
FSTAT = 30.96 SIG LVL = .0000									
FSTAT = 21.38 SIG LVL = .0000									
RSQ									
DF									
.0345									
40									
.1770									
4392									

STAGE		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS		NO.		SYS	
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		RAW SCORE WEIGHTS FOR THE NEW SYSTEM				REGRESSION CONSTANT = -42.6322	

		1	2	3	4	5	

2 SINGLE MEMBER SYSTEMS				1	4
.....					
STAGE = 4					
OVERALL RSQ = .7663					
.....					
F-TEST FOR THE EQUALITY OF REGRESSION PARAMETERS					
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SYSTEMS					
GROUPING THIS STAGE					
.....					
FOR SYS'S COMBINED AT THIS STAGE					
.....					
FOR SYS'S COMBINED UP TO THIS STAGE					

IDENT MEMBERS CASES		MS4	CHANGE FROM 5 SYSTEMS		RESIDUAL	CHANGE FROM 9 SYSTEMS		RESIDUAL
6	2	996 .7701	MS4	.0217	.2115	MS4	.0562	.1770

RAW SCORE WEIGHTS FOR THE NEW SYSTEM		2	REGRESSION CONSTANT = -42.6322						
1	.0699	.5247	.0710	.0086					
2	.0376	.5737	.1013	.0119					
3	.0376	.5737	.1013	.0119					
4	.0376	.5737	.1013	.0119					
5	.0376	.5737	.1013	.0119					
6	.0376	.5737	.1013	.0119					
7	.0376	.5737	.1013	.0119					
8	.0376	.5737	.1013	.0119					
9	.0376	.5737	.1013	.0119					
10	.0376	.5737	.1013	.0119					
11	.0376	.5737	.1013	.0119					
12	.0376	.5737	.1013	.0119					
13	.0376	.5737	.1013	.0119					
14	.0376	.5737	.1013	.0119					
15	.0376	.5737	.1013	.0119					
16	.0376	.5737	.1013	.0119					
17	.0376	.5737	.1013	.0119					
18	.0376	.5737	.1013	.0119					
19	.0376	.5737	.1013	.0119					
20	.0376	.5737	.1013	.0119					

COMPUTER OUTPUT FROM HIER-GRP SAMPLE PROBLEM									
DATE 020378				PAGE		5			
8	2	976	.5950	DF	10	4432	DF	50	4392
DECISION VALUE = .0217 FSTAT = 45.46 SIG LVL = .0000 FSTAT = 27.87 SIG LVL = .0000									
SYSTEMS SUMMARY ROSTER									
STAGE SYS NO. NO. SYS									
IDENT LOSS MEMBERS RSQ CASES IDENT IDENTIFICATION OF OTHER MEMBERS									
5	.0165	3	.8030	1494	2	5	3		
4	.0397	4	.6258	1992	6	7	8	9	
DELTA WEIGHTS FOR THE NEW SYSTEM 6 NEW SYS CRITERION MEAN = 56.6621									
NEW SYS CRITERION SD = 16.3052									
1	.2403	2	.3858	.1177	.1367	-.1056	.0714	.0416	.0570
RAW SCORE WEIGHTS FOR THE NEW SYSTEM 6 REGRESSION CONSTANT = -23.9405									
1	.0244	2	.8932	.1257	.0151	.0626	2.5717	2.0395	-3.6167
2 SINGLE MEMBER SYSTEMS 1 4									
STAGE = 3 OVERALL RSQ = .7406									
F-TTEST FOR THE EQUALITY OF REGRESSION PARAMETERS									
SYSTEMS									
GROUPING THIS STAGE FOR SYS'S COMBINED AT THIS STAGE FOR SYS'S COMBINED UP TO THIS STAGE									
SYS NO. NO. SYS	CHANGE FROM								
IDENT MEMBERS CASES RSQ	4 SYSTEMS RESIDUAL 9 SYSTEMS RESIDUAL								
1 1 498 .9247	RSQ	.0262	2332	RSQ	.0823	.1770	4392		
2 3 1494 .6030	DF	10	4442	DF	60	4392			
DECISION VALUE = .0262 FSTAT = 49.88 SIG LVL = .0000 FSTAT = 34.05 SIG LVL = .0000									
SYSTEMS SUMMARY ROSTER									
STAGE SYS NO. NO. SYS									
IDENT LOSS MEMBERS RSQ CASES IDENT IDENTIFICATION OF OTHER MEMBERS									
3	.0427	4	.7907	1992	1	2	5	3	
BETA WEIGHTS FOR THE NEW SYSTEM 1 NEW SYS CRITERION MEAN = 62.3640									
NEW SYS CRITERION SD = 20.0343									
1	.4755	2	.1553	.3002	.0738	-.0236	.0307	.0224	.0055
RAW SCORE WEIGHTS FOR THE NEW SYSTEM 1 REGRESSION CONSTANT = -35.6910									
1	.0594	2	.0622	.0100	.1963	1.7068	.2431		
4	.0397	4	.6258	1992	6	7	8	9	
1 SINGLE MEMBER SYSTEMS 4									
STAGE = 2 OVERALL RSQ = .6828									
F-TTEST FOR THE EQUALITY OF REGRESSION PARAMETERS									

SYSTEMS		FOR SYS'S COMBINED AT THIS STAGE		FOR SYS'S COMBINED UP TO THIS STAGE	
GROUPING THIS STAGE					
NO.	NO.	CHANGE FROM		CHANGE FROM	
9	9	3 SYSTEMS		9 SYSTEMS	
1	1	RSQ	RESIDUAL	RSQ	RESIDUAL
4	4	1992 .7907	.2594	.1402	.1770
6	6	1992 .6258	10	70	4392
DECISION VALUE =	.0578	FSTAT =	99.23 SIG LVL = .0000	FSTAT =	49.67 SIG LVL = .0000

[illegible]

I SINGLE MEMBER SYSTEMS									
STAGE = 1 OVERALL RSQ = .6084									
F-TTEST FOR THE EQUALITY OF REGRESSION PARAMETERS									
SYSTEMS									
GROUPING THIS STAGE		FOR SYS'S COMBINED AT THIS STAGE		FOR SYS'S COMBINED UP TO THIS STAGE					
SYS NO.	NO.	CHANGE FROM		CHANGE FROM					
IDENT MEMBERS	CASES	RSQ	2 SYSTEMS	RESIDUAL	9 SYSTEMS	RESIDUAL			
1	8	3984	.6636	RSQ	.3172	RSQ	.2146	.1770	
4	1	496	.7072	DF	10	DF	80	4392	
DECISION VALUE=		.0745		FSTAT= 104.75		SIG LVL= .0000		FSTAT= 66.56 SIG LVL= .0000	

SYSTEMS SUMMARY ROSTER													
STAGE	SYS	NO.	SYS	IDENTIFICATION OF OTHER MEMBERS									
IDENT	LOSS	MEMBERS	RSQ	CASES	IDENT	1	2	3	6	7	8	9	4
1	.2146	9	.6083	4482	1	2	5	3	6	7	8	9	4
NEW SYS CRITERION MEAN = 60.9054													
NEW SYS CRITERION SD = 18.8968													
REGRESSION CONSTANT = -29.0207													
BETA WEIGHTS FOR THE NEW SYSTEM 1													
RAW SCORE WEIGHTS FOR THE NEW SYSTEM 1													
REGRESSION CONSTANT = -29.0207													
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REGRESSION CONSTANT = -29.0207													
BETA WEIGHTS FOR THE NEW SYSTEM 1													
RAW SCORE WEIGHTS FOR THE NEW SYSTEM 1													
REGRESSION CONSTANT = -													

END OF JUNE

APPENDIX D: HIER-GRP SOURCE LISTING

SOURCE LISTING FOR HIER-GRP DRIVER (MAIN) PROGRAM HG-MAIN

1:C BLJ# ABCDEFGHIJKLMNOPQRSTUVWXYZ-<->68*(%:?:/0123456789'\\"/>

2:C THE ABOVE LINE IS THE UNIVAC 1100 CHARACTER SET (OCTAL 00 - 77)

3:C-----

4:C SECTION 1)

5:C

6:C

HIER-GRP

7:C A COMPUTER PROGRAM FOR THE HIERARCHICAL GROUPING OF REGRESSION EQUATIONS

8:C-----

9:C SECTION 2)

10:C

11:C

12:C

13:C

14:C

15:C

16:C

17:C

18:C

19:C

20:C

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SECTION 1) HIER-GRP TITLE

SECTION 2) TABLE OF CONTENTS

SECTION 3) ALGORITHM DESCRIPTION

SECTION 4) REQUIRED INFORMATION FOR USERS

SECTION 5) HOW TO USE HIER-GRP

SECTION 6) PROGRAMS IN THE HIER-GRP PACKAGE

SECTION 7) VARIABLE DESCRIPTIONS

SECTION 8) HIER-GRP DRIVER PROGRAM

21:C SECTION 3)

22:C

23:C

24:C

25:C

26:C

27:C

28:C

29:C

30:C

31:C

32:C

33:C

34:C

ALGORITHM DESCRIPTION

THE BASIC IDEA OF THE HIER-GRP ALGORITHM IS TO REDUCE A SET OF REGRES-
 SION EQUATIONS (ALSO CALLED SYSTEMS), COMPUTED FROM PROPORTIONAL PREDIC-
 TOR SONS OF CROSS PRODUCTS MATRICES, TO A SINGLE EQUATION. AT EACH STEP
 THE NUMBER OF EQUATIONS IS REDUCED BY ONE. THIS IS ACCOMPLISHED BY RE-
 PLACING TWO EQUATIONS WITH A COMPROMISE EQUATION. THE REMAINING EQUATIONS
 TOGETHER WITH THE COMPROMISE EQUATION FORM THE POOL FOR THE NEXT REPLACE-
 MENT. THE TWO EQUATIONS REPLACED ARE REFERRED TO AS THE MEMBERS OF THE
 COMPROMISE SYSTEM. IF TWO COMPROMISE EQUATIONS ARE REPLACED, THEN THE
 MEMBERS OF EACH COMPROMISE EQUATION BECOME MEMBERS OF THE NEW COMPROMISE
 SYSTEM. THE CRITERION FOR SELECTING THE TWO EQUATIONS TO BE REPLACED IS
 THE SAME AT EVERY STEP. THE PROGRAM HAS SIX GROUPING CRITERIA, ONE OF

35:C WHICH MUST BE SPECIFIED BY THE USER. ALL THE GROUPING CRITERIA MAY BE
 36:C VIEWED AS BEING CONCEPTUALLY THE SAME. IN EACH CASE THE REPLACEMENT OF
 37:C TWO EQUATIONS BY A COMPROMISE EQUATION IS ASSOCIATED WITH A LOSS; THOUGH
 38:C THE LOSS AND THE METHOD USED TO COMPUTE THE LOSS ARE DIFFERENT FOR EACH.
 39:C THE PAIR OF EQUATIONS TO BE REPLACED IS THE PAIR HAVING THE SMALLEST OR
 40:C LARGEST ASSOCIATED LOSS DEPENDING ON WHETHER IT IS DESIRED TO GROUP TO-
 41:C GETHER SIMILAR OR DISSIMILAR EQUATIONS. THE SIX CRITERIA ARE LISTED IN
 42:C THE FOLLOWING TABLE.
 43:C
 44:C

GROUPING CRITERIA AVAILABLE IN HIER-GRP

GROUPING OPTION	LOSS ASSOCIATED WITH REPLACEMENT OF SYS'S I AND J	GROUPING CRITERIA
1 **	LOSS = DECREASE IN THE SQUARED MULTIPLE CORRELATION COEFFICIENT, R_{SQ} , UNDER THE HYPOTHESIS THAT THE BETA WEIGHTS FOR EQU I EQUAL THE CORRESPONDING WEIGHTS FOR EQU J.	(MAX LOSS)

6 **	LOSS = SAME AS FOR 1.	(MINIMIZE LOSS)
3 **	LOSS = WEIGHTED AVERAGE OF LOSSES FOR ALL COMBINATIONS OF A MEMBER OF SYS I WITH A MEMBER OF SYS J, WHERE FOR A GIVEN COMBINATION THE WEIGHT IS THE PRODUCT OF THE NUMBER OF CASES IN EACH MEMBER OF THE COMBINATION AND THE LOSS IS THE DECREASE IN R_{SQ} UNDER THE HYPOTHESIS THAT THE CORRESPONDING BETA WEIGHTS FOR EACH MEMBER OF THE COMBINATION ARE EQUAL.	(MAX LOSS)

5 **	LOSS = SAME AS FOR 3.	(MINIMIZE LOSS)
2 **	LOSS = MINIMUM OF LOSSES FOR ALL COMBINATIONS OF A MEMBER OF EITHER SYS I OR SYS J WITH A DIFFERENT MEMBER OF EITHER SYS I OR SYS J, WHERE FOR A GIVEN COMBINATION THE LOSS IS THE DECREASE IN R_{SQ} UNDER THE HYPOTHESIS THAT THE CORRESPONDING BETA WEIGHTS FOR EACH MEMBER OF THE COMBINATION ARE EQUAL.	(MAX LOSS)

4 **	LOSS = SAME AS FOR 2 BUT WITH MAXIMUM REPLACING MINIMUM AS THE FIRST WORD OF THE DESCRIPTION.	(MINIMIZE LOSS)
------	--	-----------------

68:C-----
 69:C SECTION 4)
 70:C

REQUIRED INFORMATION FOR USERS

71:C	-----
72:C	FOR EACH EQUATION, THE FOLLOWING INFORMATION IS REQUIRED:
73:C	1. THE NUMBER OF CASES(OBSERVATIONS)
74:C	2. THE CRITERION MEAN AND STANDARD DEVIATION
75:C	3. THE STANDARDIZED REGRESSION WEIGHTS
76:C	4. THE VALIDITY COEFFICIENTS
77:C	5. THE MEANS AND STANDARD DEVIATIONS OF THE PREDICTORS.
78:C	IT IS IMPORTANT TO REALIZE THAT THE HIER-GRP ALGORITHM REQUIRES ALL THE
79:C	REGRESSION EQUATIONS TO BE LEAST SQUARES SOLUTIONS DERIVED FROM
80:C	PROPORTIONAL PREDICTOR SUMS OF CROSS PRODUCTS MATRICES (I.E., THE MEAN
81:C	OF A PREDICTOR FOR ONE EQUATION MUST EQUAL THE MEAN OF THE CORRESPONDING
82:C	PREDICTORS IN ALL OTHER EQUATIONS. IN ADDITION THE COVARIANCE MATRICES
83:C	FOR EACH EQUATION MUST BE IDENTICAL.). THIS IS THE PROPORTIONALITY
84:C	ASSUMPTION OF BOTTERBERG AND CHRISTAL (WADD-TN-61-30).
85:C	-----
86:C	SECTION 5)
87:C	HOW TO USE HIER-GRP
88:C	-----
89:C	TO EXECUTE THIS PROGRAM THE USER MUST PREPARE THE FOLLOWING SEQUENCE
90:C	OF CONTROL CARDS AND DATA CARDS:
91:C	1. CONTROL CARD.
92:C	CARD FORMAT
93:C	COLUMNS FORMAT DESCRIPTION
94:C	1-3 13 REQS, NUMBER OF REGRESSION EQUATIONS(SYSTEMS) TO BE
95:C	GROUPED
96:C	REQS MUST BE .LE. 50
97:C	4-6 13 NPREDs, NUMBER OF PREDICTOR VARIABLES IN EACH
98:C	EQUATION, I.E., NUMBER OF BETA WEIGHTS(STANDARDIZED
99:C	REGRESSION WEIGHTS) IN EACH EQUATION.
100:C	NPREDs MUST BE .LE. 100
101:C	7 11 IOPT, THE GROUPING OPTION DESIRED. NORMALLY OPTION
102:C	'6' IS SPECIFIED WHICH CAUSES THE GROUPING TO BE
103:C	DONE BASED ON THE ITERATIVE TECHNIQUE DEVELOPED BY
104:C	POTTERBERG AND CHRISTAL, WADD-TN-61-30.
105:C	SEE SECTION 3 FOR MORE INFORMATION
106:C	8 11 ENDRS, NUMBER OF HEADER(LABEL,TITLE) CARDS THAT

107:C	FOLLOW THIS CONTROL CARD. THE NUMBER OF HEADER		
108:C	CARDS CAN RANGE FROM 0 TO 9.		
109:C	9	11	I READ, THE DATA READ OPTION. I READ = 0 MEANS
110:C	READ THE BETA WEIGHTS AND VALIDITIES NPRED		
111:C	ITEMS AT A TIME. I READ = 1 MEANS READ THEM		
112:C	NEQS*NPRED ITEMS AT A TIME.		
113:C	2. HEADER CARD(S)		
114:C	CARD	FORTAN	
115:C	COLUMNS	FORMAT	DESCRIPTION
116:C	1-80	13A6,A2	EACH HEADER CARD CONTAINS UP TO 80 ALPHANUMERIC
117:C	CHARACTERS WHICH ARE PRINTED(80 CHARACTERS/LINE) AT		
118:C	THE BEGINNING OF THE GROUPING REPORT. HEADER CARDS		
119:C	CAN BE OMITTED, OR UP TO 9 CARDS CAN BE USED,		
120:C	DEPENDENT UPON THE NUMBER(NHDRS) SPECIFIED IN THE		
121:C	INITIAL CONTROL CARD. THE NUMBER OF HEADER CARDS		
122:C	PRESENT MUST EQUAL NHDRS.		
123:C	3. FORMAT CARD TO READ THE NUMBER OF CASES FOR EACH EQUATION		
124:C	CARD	FORTAN	
125:C	COLUMNS	FORMAT	DESCRIPTION
126:C	1-80	13A6,A2	THE FORTAN VARIABLE FORMAT BY WHICH THE SN(I) ARE
127:C	TO BE READ. SN(I) DENOTES THE NUMBER OF CASES THAT		
128:C	WERE USED IN THE COMPUTATION OF EQUATION I. FOR		
129:C	EXAMPLE, IF 10 EQUATIONS ARE TO BE GROUPED(NEQS=10)		
130:C	THE FORMAT CARD MIGHT BE '(10F5.0)'. THE F EDIT		
131:C	CODE MUST BE USED SINCE SN(I) IS A REAL VARIABLE.		
132:C	4. SN(I) DATA CARD(S)		
133:C	CARD	FORTAN	
134:C	COLUMNS	FORMAT	DESCRIPTION
135:C	*** DATA IS READ ACCORDING TO PREVIOUS FORMAT		
136:C	5. FORMAT CARD TO READ CRITERION MEANS AND STANDARD DEVIATIONS		
137:C	CARD	FORTAN	
138:C	COLUMNS	FORMAT	DESCRIPTION
139:C	1-80	13A6,A2	THE FORTAN VARIABLE FORMAT BY WHICH THE SM(I) AND
140:C	THE SSD(I) DATA ARE TO BE READ. SM(I) DENOTES THE		
141:C	CRITERION MEAN FOR EQUATION I. SSD(I) DENOTES THE		
142:C	CRITERION STANDARD DEVIATION FOR EQUATION I. FOR		

143:C	EXAMPLE, IF 10 EQUATIONS ARE TO BE GROUPED (NEQS=10)		
144:C	THE 10 PAIRS OF SM(I) AND SSD(I) MIGHT BE READ WITH		
145:C	THE FOLLOWING FORMAT CARD:*(1UX,F10.4,5X,F10.4)*.		
146:C	6. SM(I) AND SSD(I) DATA CARDS.		
147:C	CARD	FORTRAN	
148:C	COLUMNS	FORMAT	DESCRIPTION
149:C	*** DATA IS READ ACCORDING TO PREVIOUS FORMAT.		
150:C	7. FORMAT CARD TO READ BETA WEIGHTS FOR EACH EQUATION.		
151:C	CARD	FORTRAN	
152:C	COLUMNS	FORMAT	DESCRIPTION
153:C	1-80	13A6,A2	THE FORTRAN VARIABLE FORMAT BY WHICH THE BETA
154:C			WEIGHTS FOR EACH EQUATION ARE READ. THE BETA
155:C			WEIGHTS(NPRED'S WEIGHTS PER EQUATION) ARE STORED IN
156:C			THE B(I) ARRAY. THE FIRST NPRED'S ELEMENTS OF B
157:C			CONTAIN THE BETA WEIGHTS FOR EQUATION 1, THE NEXT
158:C			NPRED'S ELEMENTS CONTAIN THE BETA WEIGHTS FOR
159:C			EQUATION 2, AND SO ON. THE WEIGHTS FOR EACH
160:C			EQUATION ARE STORED IN VARIABLE NUMBER ORDER.
161:C	8. BETA WEIGHT DATA CARDS.		
162:C	CARD	FORTRAN	
163:C	COLUMNS	FORMAT	DESCRIPTION
164:C	*** THE BETA WEIGHTS ARE READ ACCORDING TO THE PREVIOUS FORMAT.		
165:C	9. FORMAT CARD TO READ VALIDITY COEFFICIENTS FOR EACH EQUATION.		
166:C	CARD	FORTRAN	
167:C	COLUMNS	FORMAT	DESCRIPTION
168:C	1-80	13A6,A2	THE FORTRAN VARIABLE FORMAT BY WHICH THE VALIDITY
169:C			COEFFICIENTS (CORRELATIONS BETWEEN THE PREDICTOR
170:C			VARIABLES AND THE CRITERION VARIABLE) FOR EACH
171:C			EQUATION ARE TO BE READ. THE VALIDITY COEFFICIENTS
172:C			(NPRED'S COEFFICIENTS PER EQUATION) ARE STORED IN
173:C			THE V(I) ARRAY. THE FIRST NPRED'S ELEMENTS OF V
174:C			CONTAIN THE VALIDITIES FOR EQUATION 1, THE NEXT
175:C			NPRED'S ELEMENTS CONTAIN THE VALIDITIES FOR EQUATION
176:C			2, AND SO ON. THE VALIDITIES FOR EACH EQUATION ARE
177:C			STORED IN VARIABLE NUMBER ORDER.
178:C	10. THE VALIDITY COEFFICIENT DATA CARDS.		

179:C	CARD	FORTAN	DESCRIPTION
180:C	COLUMNS	FORMAT	
181:C	***	THE VALIDITIES ARE READ ACCORDING TO THE PREVIOUS FORMAT.	
182:C	11.	FORMAT CARD TO READ PREDICTOR MEANS AND STANDARD DEVIATIONS.	
183:C	CARD	FORTAN	
184:C	COLUMNS	FORMAT	
185:C	1-80	13A6,A2	THE FORTAN VARIABLE FORMAT BY WHICH THE PM(L) AND PSD(L) DATA ARE TO BE READ. PM(L) DENOTES THE MEAN OF THE PREDICTOR VARIABLE L. PSD(L) DENOTES THE STANDARD DEVIATION OF PREDICTOR VARIABLE L.
186:C			
187:C			
188:C			
189:C			
190:C	12.	PM(L) AND PSD(L).DATA CARDS.	
191:C	CARD	FORTAN	
192:C	COLUMNS	FORMAT	
193:C	***	DATA IS READ ACCORDING TO PREVIOUS FORMAT.	
194:C	13.	REPEAT 1 - 12 ABOVE AS OFTEN AS DESIRED, THEN INCLUDE A BLANK CARD AS THE LAST CARD IN THE DECK.	
195:C			
196:C			
197:C	SECTION 6)		
198:C		PROGRAMS IN THE HIER-GRP PACKAGE	
199:C			
200:C	6.1	HG-MAIN.	FORTAN MAIN PROGRAM. PACKAGE DRIVER - READS
201:C			CONTROL CARD, INPUT DATA, CALLS REMAINING ROUTINES.
202:C	6.2	START.	ASSEMBLER SUBROUTINE. RESETS PAGE MARGINS ON
203:C			THE PRINTER TO 0 LINES AT TOP, 0 LINES AT BOTTOM.
204:C	6.3	OVRLP.	FORTAN SUBROUTINE. COMPUTES THE OVERLAP
205:C			VECTOR, A, FOR USE IN GROUP.
206:C	6.4	GROUP.	FORTAN SUBROUTINE. PERFORMS THE GROUPING
207:C			PROCEDURE.
208:C	6.5	STAGE.	FORTAN SUBROUTINE. COMPUTES THE GROUPING
209:C			OUTPUT.
210:C	6.6	PRINTG.	FORTAN SUBROUTINE. PRINTS THE GROUPING
211:C			REPORT.
212:C	6.7	PLEVEL.	FORTAN SUBROUTINE. CALCULATES THE PROB-
213:C			ABILITY OF THE F-RATIO TEST STATISTIC.
214:C			

215:C	SECTION 7)	
216:C		VARIABLE DESCRIPTIONS
217:C		-----
218:C	NEQS = NUMBER OF REGRESSION EQUATIONS TO BE GROUPED.	
219:C	NPREDs = NUMBER OF BETA WEIGHTS IN EACH EQUATION.	
220:C	IOPT = GROUPING OPTION SWITCH. (SEE SECTION 3, AND 5 ABOVE FOR DETAILS)	
221:C	IREAD = THE DATA READ OPTION. (SEE SECTION 5)	
222:C	NHDRS = NUMBER OF CARDS IN HEADER LABEL. (MUST BE LESS THAN 10)	
223:C	FMT = FORMAT AREA.	
224:C	SN = VECTOR OF N'S. SN(I) IS THE NUMBER OF CASES IN SYSTEM I.	
225:C	REQUIRED SIZE - NEQS.	
226:C	SM = VECTOR OF CRITERION MEANS. SM(I) IS THE CRITERION MEAN FOR SYSTEM I.	
227:C		
228:C	REQUIRED SIZE - NEQS.	
229:C	SSD = VECTOR OF CRITERION STANDARD DEVIATIONS. SSD(I) IS THE CRITERION STANDARD DEVIATION FOR SYSTEM I.	
230:C		
231:C	REQUIRED SIZE - NEQS.	
232:C	B = VECTOR OF BETA WEIGHTS. B(IL) IS THE BETA WEIGHT FOR PREDICTOR L IN SYSTEM I, WHERE IL=NPREDs*(I-1)+L.	
233:C		
234:C	REQUIRED SIZE - NEQS*NPREDs.	
235:C	V = VECTOR OF VALIDITIES. V(IL) IS THE CORRELATION BETWEEN PREDICTOR L AND THE CRITERION VARIABLE FOR SYSTEM I, WHERE IL IS AS IN B.	
236:C		
237:C	REQUIRED SIZE - NEQS*NPREDs.	
238:C	PM = VECTOR OF PREDICTOR MEANS. PM(L) IS THE MEAN OF PREDICTOR VARIABLE L.	
239:C		
240:C	REQUIRED SIZE - NPREDs.	
241:C	PSD = VECTOR OF STANDARD DEVIATIONS OF PREDICTOR VARIABLES.	
242:C	PSD(L) IS THE STANDARD DEVIATION FOR PREDICTOR VARIABLE L.	
243:C	REQUIRED SIZE - NPREDs.	
244:C	A = THE OVERLAP VECTOR (COMPUTED IN SUBROUTINE OVRLP). A(IJ) IS THE OVERLAP OR DECISION VALUE IF SYSTEMS I AND J ARE GROUPED, WHERE IJ=NEQS*(I-1) - I*(I-1)/2 + (J-1). ON RETURN FROM SUBROUTINE	
245:C		
246:C	OVRLP A(IJ) IS THE DROP IN RSQ WHEN SYSTEM I IS COMBINED WITH SYSTEM J. SUBROUTINE GROUP USES THE A VECTOR TO PERFORM THE GROUPING PROCEDURE.	
247:C		
248:C		
249:C		
250:C	REQUIRED SIZE - NEQS*(NEQS-1)/2.	

251:C Z = WORK AREA USED IN OVRLP, GROUP, AND PRINTG. ON RETURN FROM GROUP
 252:C Z(KU) IS THE DECISION VALUE FOR THE GROUPING THAT OCCURED AT THE
 253:C KU SYSTEM STAGE.
 254:C REQUIRED SIZE - NEQS.
 255:C IU = VECTOR OF ABSORBING SYSTEM ID'S(COMPUTED IN GROUP). IU(KU) IS
 256:C THE ID OF THE ABSORBING SYSTEM SELECTED AT THE KU SYSTEM STAGE.
 257:C REQUIRED SIZE - NEQS.
 258:C JU = VECTOR OF ABSORBED SYSTEM ID'S(COMPUTED IN GROUP). JU(KU) IS THE
 259:C ID OF THE ABSORBED SYSTEM SELECTED AT THE KU SYSTEM STAGE.
 260:C REQUIRED SIZE - NEQS.
 261:C SR = VECTOR OF RSW'S(COMPUTED IN STAGE). SR(I) IS THE RSQ ASSOCIATED
 262:C WITH REGRESSION EQUATION I.
 263:C REQUIRED SIZE - NEQS.
 264:C ORU = VECTOR OF RSW'S(COMPUTED IN STAGE). ORU(KU) IS THE OVERALL RSQ
 265:C AT THE KU SYSTEM STAGE.
 266:C REQUIRED SIZE - NEQS.
 267:C SRU = VECTOR OF RSW'S(COMPUTED IN STAGE). SRU(KU) IS THE RSQ FOR THE
 268:C PAIR OF SYSTEMS, IU(KU) AND JU(KU), GROUPING AT THE KU SYSTEM
 269:C STAGE.
 270:C REQUIRED SIZE - NEQS.
 271:C KP = VECTOR OF SYSTEM ID'S(COMPUTED IN STAGE). KP(I) IS THE ID OF THE
 272:C SYSTEM FOLLOWING SYSTEM I IN THE FINAL HIERARCHICAL ORDERING.
 273:C REQUIRED SIZE - NEQS.
 274:C KS = INVERSE OF JU(COMPUTED IN PRINTG). IF JU(KU)=J THEN KS(J)=KU.
 275:C REQUIRED SIZE - NEQS.
 276:C KU = VECTOR OF SYSTEM ID'S USED IN PRINTG TO STORE THE MEMBERS OF EACH
 277:C SYSTEM AT EACH STAGE.
 278:C REQUIRED SIZE - NEQS.
 279:C BET() = WORK AREA, USED TO STORE BETA WEIGHTS FOR STEPWISE PRINTING
 280:C IN SUBROUTINE PRINTG.
 281:C REQUIRED SIZE - IMPREDS.
 282:C-----
 283:C SECTION 8)
 284:C
 285:C HIER-GRP PACKAGE DRIVER
 286:C-----
 THE PURPOSE OF THIS PROGRAM IS:

```

287:C 1. READ AND PRINT CONTROL CARD.
288:C 2. READ AND PRINT INPUT DATA (NUMBER OF CASES, CRITERION MEANS AND
289:C STANDARD DEVIATIONS, BETA WEIGHTS, VALIDITIES, AND PREDICTOR MEANS
290:C AND STANDARD DEVIATIONS).
291:C 3. CALL ROUTINES TO: A) COMPUTE OVERLAP MATRIX, B) PERFORM GROUPING
292:C PROCEDURE, C) COMPUTE GROUPING OUTPUT, AND D) PRINT GROUPING REPORT.
293:C -----
294:C
295: PARAMETER EQS=50, PKDS=100, BV DIM=EQS*PKDS, ADIM=(EQS-1)/2
296:C MAXIMUM OF 50 EQUATIONS AND 100 PREDICTORS ALLOWED BY PARAMETER STATEMENT
297: DIMENSION SN(EQS), SR(EQS), SSD(EQS), B(BV DIM), V(BV DIM), PM(PKDS),
298: IPSD(PKDS), A(ADIM), Z(EQS), IU(EQS), JU(EQS), SR(EQS), ORU(EQS),
299: ZSRU(EQS), KP(EQS), KS(EQS), KO(EQS), FMT(14), BE(PKDS)
300:C RESET PAGE MARGINS TO 0 LINES AT TOP, 0 LINES AT BOTTOM
301: CALL START
302:C
303:C READ AND PRINT INITIAL CONTROL CARD
304:I READ(5,500,END=1000) NEQS, NPRED, IOPT, NHDRS, IREAD
305: 500 FORMAT(213,311)
306: IF(NEQS.EQ.0) GO TO 900
307:C START, SKIP TO A NEW PAGE
308: PRINT 598
309: 598 FORMAT(1H1/20X,'HIERARCHICAL GROUPING PROGRAM HIER-GRP'//
310: 1 80X,'COMPUTATIONAL SCIENCES DIVISION'//
311: 2 80X,'AF HUMAN RESOURCES LABORATORY'//
312: 3 80X,'AIR FORCE SYSTEMS COMMAND'//
313: 4 20X,'VERSION DATE 11 JAN 1978')
314: PRINT 600, NEQS, JPRED, IOPT, NHDRS
315: 600 FORMAT('1. CONTROL CARD PARAMETERS',/6X,23(1H-),
316: 1//'NUMBER OF REGRESSION EQUATIONS = ',12,5X,
317: 1'NUMBER OF PREDICTOR VARIABLES = ',12/1X,
318: 2'GROUPING OPTION = ',11,5X,
319: 4'NUMBER OF HEADER CARDS = ',11)
320: IF(NEQS.LT.2) GO TO 901
321: IF((IOPT.LT.1).OR.(IOPT.GT.6)) GO TO 901
322: IF(NHDRS.EQ.0) GO TO 3

```



```

323:C      READ AND PRINT HEADER CARDS
324:      PRINT 597
325: 597 FORMAT(/6X,'PROBLEM HEADER LABEL',/6X,20(1H-)/)
326:      DO 2 I=1,NHDRS
327:      READ 501,FMT
328:      501 FORMAT(13A6,A2)
329:      PRINT 604,FMT
330:      604 FORMAT(1H,13A6,A2)
331:2      CONTINUE
332:C      DATA INPUT
333:3      PRINT 596
334: 596 FORMAT(/' 11.  FORMAT CARDS AND INPUT DATA',/6X,2/(1H-))
335:      READ 501,FMT
336:      PRINT 605,FMT
337: 605 FORMAT(/' FORMAT TO READ SN(I) = ',13A6,A2)
338:      READ FMT,(SN(I),I=1,NEQS)
339:C
340:      READ 501,FMT
341:      PRINT 606,FMT
342: 606 FORMAT(/' FORMAT TO READ SM(I) AND SSD(I) = ',13A6,A2)
343:      PRINT 607
344: 607 FORMAT(/' EQUATION      N      CRITERION MEAN      CRITERION SD')
345:      READ FMT,(SM(I),SSD(I),I=1,NEQS)
346:      PRINT 608,(I,SN(I),SM(I),SSD(I),I=1,NEQS)
347: 608 FORMAT(1H,18,F12.0,F16.5,F15.5)
348:C
349:      IEP = NEQS * NPRED5
350:      MIN = MIN0( 15,NPRED5 )
351:      READ 501,FMT
352:      PRINT 609,FMT
353: 609 FORMAT(/' FORMAT TO READ BETA WEIGHTS = ',13A6,A2)
354:      PRINT 610, ( I, I = 1, MIN )
355: 610 FORMAT(' BETA WEIGHTS',15,1418)
356:      IF ( IREAD .NE. 0 ) READ FMT,( B(I), I = 1,IEP )
357:      IE=0
358:      DO 4 I=1,NEQS

```



```

359:      IS=IE+1
360:      IE=IE+NPRED5
361:      IF ( IREAD .EQ. 0 ) READ FMT, (B(J),J=15,IE)
362:      PRINT 611,I,(B(J),J=15,IE)
363:      FORMAT( EQU ' ,13,2X,15F8.4,14(/10X,15F8.4) )
364:      CONTINUE
365: C
366:      READ 501,FMT
367:      PRINT 612,FMT
368:      FORMAT(//' FORMAT TO READ VALIDITIES = ',13A6,A2)
369:      PRINT 613, ( I, I = 1, MIN )
370:      FORMAT( ' VALIDITIES',17,14I8)
371:      IF ( IREAD .NE. 0 ) READ FMT, ( V(I), I = 1,IEP )
372:      IE=0
373:      DO 5 I=1,NEQS
374:      IS=IE+1
375:      IE=IE+NPRED5
376:      IF ( IREAD .EQ. 0 ) READ FMT, (V(J),J=15,IE)
377:      PRINT 611,I,(V(J),J=15,IE)
378:      CONTINUE
379: C
380:      READ 501,FMT
381:      PRINT 614,FMT
382:      FORMAT(//' FORMAT TO READ PH(L) AND PSD(L) = ',13A6,A2)
383:      PRINT 615
384:      FORMAT(//' PREDICTOR',10X,'PREDICTOR MEAN',10X,'PREDICTOR SD')
385:      READ FMT, (PH(L), PSD(L), L = 1,NPRED5)
386:      DO 617 L = 1,NPRED5
387:      PRINT 616, L, PH(L), PSD(L)
388:      FORMAT(1H ,16,3X,'X',F18.5,4X,F18.5)
389: C      COMPUTE OVERLAP MATRIX
390:      CALL OVRLEP(NEWS,NPRED5,SN,SD,SSD,B,V,A,Z)
391: C      PERFORM GROUPING PROCEDURE
392:      CALL GROUP(IOPT,NEWS,SN,A,Z,IU,JU)
393: C      COMPUTE STAGE VALUES
394:      CALL STAGE(NEWS,NPRED5,SN,SD,SSD,B,V,IU,JU,SR,ORU,SRU,KP)

```

	PRINT GROUPING REPORT
395:C	
396:	CALL PRINTG
397:	1(IUPT,NEWS,HPREDS,SU,SM,SSU,3,PM,PSD,2,IU,JU,SR,ORU,SRU,
398:	2 KS,KP,KU,A,BE)
399:C	RETURN TO START
400:	GO TO 1
401:C	END OF JOB
402:	900 PRINT 601
403:	601 FORMAT('1END OF JOB')
404:	STOP
405:C	CONTROL CARD ERROR
406:	901 PRINT 602
407:	602 FORMAT('1CONTROL CARD ERROR')
408:	STOP
409:C	END OF CARD FILE
410:	1000 PRINT 603
411:	603 FORMAT('1END OF CARD FILE')
412:	STOP
413:	END

SOURCE LISTING FOR HIER-GNP SUBROUTINE START

```

1: AXAP .      ASSEMBLER LANGUAGE ROUTINE
2: IMAGE .M,60,U,U. .
3: START .
4: LA AU,(2,IMAGE) .
5: ER PRTCNB .
6: J I,X11 .
7: END .
  
```

SOURCE LISTING FOR HIER-GNP SUBROUTINE OVRLP

```

1:C-----
2:C
3:C SUBROUTINE OVRLP
4:C-----
5:C THIS ROUTINE COMPUTES THE INITIAL VALUES OF THE OVERLAP VECTOR,
6:C A. IT IS ASSUMED THAT THE PROPORTIONALITY ASSUMPTION (SEE SECTION 3
7:C OF HG-MAIN) IS SATISFIED BY THE PREDICTOR VARIABLES; OTHERWISE THE
8:C EQUATION FOR A(IJ) FOLLOWING STATEMENT 210 IS NOT VALID.
9:C-----
10:C
11:C
12:C
13:C NEQS = NUMBER OF SYSTEMS.
14:C NPRED = NUMBER OF PREDICTOR VARIABLES.
15:C SN (I) = NUMBER OF CASES (OBSERVATIONS)
16:C SM (I) = CRITERION MEAN
17:C SSD(I) = CRITERION STANDARD DEVIATION
18:C B (IL) = STANDARD REGRESSION WEIGHT FOR PREDICTOR L IN SYSTEM I.
19:C WHERE IL = (I-1)* NPRED + L
20:C V (IL) = CRITERION CORRELATION WITH PREDICTOR L IN SYSTEM I.
  
```

VARIABLE DESCRIPTIONS

```

-----
13:C NEQS = NUMBER OF SYSTEMS.
14:C NPRED = NUMBER OF PREDICTOR VARIABLES.
15:C SN (I) = NUMBER OF CASES (OBSERVATIONS)
16:C SM (I) = CRITERION MEAN
17:C SSD(I) = CRITERION STANDARD DEVIATION
18:C B (IL) = STANDARD REGRESSION WEIGHT FOR PREDICTOR L IN SYSTEM I.
19:C WHERE IL = (I-1)* NPRED + L
20:C V (IL) = CRITERION CORRELATION WITH PREDICTOR L IN SYSTEM I.
  
```

```

21:C . WHERE IL = (I-1)*NPREDS + L
22:C A (IJ) = ORU(NEWS)-ORU(NEWS-1) OBTAINED BY PAIRING SYSTEMS I AND J.
23:C WHERE IJ = NEWS*(I-1) - I*(I-1)/2 + (J-1) AND I.LT.J
24:C Z ( ) = WORK AREA
25:C
26:C ORU(NEWS) = R SQUARED FOR NEWS SYSTEMS.
27:C ORU(NEWS-1) = R SQUARED FOR NEWS-1 SYSTEMS.
28:C-----
29:C
30:
31: I ( NEWS, NPREDS, SM, SSQ, B, V, A, Z )
32:C INPUT . . . . .
33:C OUTPUT-----UNCHANGED----- * W
34:C
35: DIMENSION SN(1), SM(1), SSQ(1), B(1), V(1), A(1), Z(1)
36:C
37: I00 ON = 0.0
38: SUMX = 0.0
39: SUMXY = 0.0
40: IL = 0
41: DO 120 I = 1,NEWS
42:C COMPUTE COMPOSITE VARIANCE, Z(I), FOR SYSTEM I .
43: SUMBV = 0.0
44: DO 110 L = 1,NPREDS
45: IL = IL + 1
46: 110 SUMBV = SUMBV + B(IL) * V(IL)
47: Z(I) = SSQ(1)**2 * SUMBV
48: ON = ON + SN(I)
49: SUMX = SUMX + SN(I) * SM(I)
50: 120 SUMXY = SUMXY + SN(I) * ( SSQ(1)**2 + SM(I)**2 )
51:C NEWS SYSTEM POOLED CRITERION VARIANCE = ONSSQ / ON .
52: ONSSQ = SUMXY - SUMX**2/ON
53: IJ = I
54: LASTI = NEWS-1
55:C
56: 200 DO 220 I = 1, LASTI

```

SUBROUTINE OVRLP


```

57:      IN      = (1 - 1) * NPRED5
58:      JN      = IN
59:      JFIRST = I + 1
60:      DO 220 J = JFIRST, NEWS
61:          SUMBV = 0.0
62:          JN    = JN + NPRED5
63:          DO 210 L = 1, NPRED5
64:              IL = L + IN
65:              JL = L + JN
66:              210 SUMBV = SUMBV + B(IL) * V(JL) + B(JL) * V(IL)
67:              A(IJ) = ( ( SN(I)*SN(J) ) / ( SN(I) + SN(J) ) )
68:                  1 * ( SSD(I)*SSD(J)*SMBV - Z(I) - Z(J) )
69:                  2 - ( SN(I) - SN(J) ) ** 2 ) / (-ONSSQ)
70:      220 IJ = IJ + 1
71:      RETURN
72:      END

```

SOURCE LISTING FOR HIER-GRP SUBROUTINE GROUP

```

1:C-----
2:C
3:C
4:C
5:C
6:C
7:C
8:C
9:C
10:C
11:C
12:C

```

SUBROUTINE GROUP

THIS ROUTINE PERFORMS THE GROUPING PROCEDURE ACCORDING TO THE
VALUE OF IOPT. IF IOPT = 1 OR 6 IT IS ASSUMED THAT THE PREDICTOR
VARIABLES SATISFY THE PROPORTIONALITY ASSUMPTION. IF IOPT = 2, 3, 4,
OR 5, THE PROPORTIONALITY ASSUMPTION DOES NOT HAVE TO HOLD. THE
GROUPING OPTIONS ARE BRIEFLY DESCRIBED BELOW (ALSO SEE SECTION 3 OF
HG-MAIN).

10:C IF IOPT = 1, MAXIMIZED Z(KU) = GRU(KU+1)-ORU(KU)
11:C IF IOPT = 6, MINIMIZED Z(KU) = ABOVE

```

13:C IF IOPT =2, MAXIMIZED Z(KU) = AVG. OF ALL NI(KU)*NJ(KU) VALUES OF
14:C A(IJ) BETWEEN IU(KU), JU(KU)
15:C IF IOPT =4, MINIMIZED Z(KU) = ABOVE
16:C IF IOPT =3, MAXIMIZED Z(KU) = MINIMUM OF ALL (NU(KU)*2-NU(KU))/2
17:C VALUES OF A(IJ) WITHIN IU(KU),JU(KU)
18:C IF IOPT =5, MINIMIZED Z(KU) = MAXIMUM OF ABOVE
19:C -----
20:C
21:C VARIABLE DESCRIPTIONS
22:C -----
23:C NEQS = NUMBER OF SYSTEMS BEFORE GROUPING (AT STAGE) .
24:C SN (1) = NUMBER OF CASES IN SYSTEM 1 AT NEWS STAGE .
25:C SN( ) VECTOR NOT USED IF IOPT = 3 OR 5
26:C A(IJ) = Z(NEQS-1) VALUE HYPOTHEZIZING IU(NEQS-1) = I, JU(NEQS-1)=J.
27:C Z(KU) = DECISION VALUE CAUSING THE SELECTION OF IU(KU), JU(KU)
28:C IU(KU) = IDENT OF SYSTEM ABSORBING SYSTEM JU(KU) AT KU STAGE.
29:C JU(KU) = IDENT OF SYSTEM GROUPING WITH SYSTEM IU(KU) AT KU STAGE
30:C KU = NUMBER OF SYSTEMS AT KU STAGE, RANGES FROM NEWS-1 TO 1 .
31:C ORU(KU) = KU SYSTEM RSQ
32:C NU(KU) = NUMBER OF MEMBERS IN SYSTEM IU(KU) AT KU STAGE.
33:C NI(KU) = NUMBER OF MEMBERS IN SYSTEM IU(KU) AT KU +1 STAGE .
34:C NJ(KU) = NUMBER OF MEMBERS IN SYSTEM JU(KU) AT KU +1 STAGE .
35:C IJ = N+I-N-(I+1+1)/2 +J, WHERE I IS ALWAYS LESS THAN J.
36:C -----
37:C
38:
39: 1 ( IOPT, NEQS, SN, A, Z, IU, JU )
40:C INPUT . . .
41:C OUTPUT ---UNCHANGED--- C . . .
42:C
43: DIMENSION SN(1), A(1), Z(1), IU(1), JU(1)
44:C
45: DO 120 K = 1, NEQS
46: Z(K) = SN(K)
47: 120 IU(K) = K
48: NGRPS = NEQS

```

SUBROUTINE GROUP

```

49:C
50: 200 BEST = -1.0E35
51: IF ( IOPT .LE. 3 ) GO TO 215
52: BEST = 1.0E35
53: 215 DO 280 KI = 1, NGRPS
54: I = IU(KI)
55: DO 280 KJ = KI, NGRPS
56: J = IU(KJ)
57: IF ( I - J ) 220,280,230
58: 220 IJ = NEWS*I-NEWS - (I*I+J)/2 + J
59: GO TO 240
60: 230 IJ = NEWS*J-NEWS - (J*J+I)/2 + I
61: 240 IF ( IOPT .GT. 3 ) GO TO 260
62: IF (BEST - A(IJ) ) 270,270,280
63: 260 IF (BEST - A(IJ) ) 260,270,270
64: 270 BEST = A(IJ)
65: IBEST = KI
66: JBEST = KJ
67: 280 CONTINUE
68:C
52
69: 300 IF ( IU(IBEST) - IU(JBEST) ) 320, 9000, 310
70: 310 KBEST = IBEST
71: IBEST = JBEST
72: JBEST = KBEST
73: 320 SNI = Z(IBEST)
74: I = IU(IBEST)
75: SNJ = Z(JBEST)
76: J = IU(JBEST)
77: Z(IBEST) = SNI + SNJ
78: Z(JBEST) = Z(IGRPS)
79: IU(JBEST) = IU(IGRPS)
80: Z(IGRPS) = BEST
81: IU(NGRPS) = I
82: JU(NGRPS) = J
83: NGRPS = NGRPS - 1
84:C

```

```

85:      DO 460 KK = 1, NGRPS
86:      K = IU(KK)
87:      SNK = Z(KK)
88:      IF (K - 1) 410,460,420
89:      410 KI = NEQS*K-NEQS - (K*K+K)/2 + I
90:      KJ = KI - I + J
91:      GO TO 450
92:      KI = NEQS*I-NEQS - (I*I+I)/2 + K
93:      IF (K*GT. J) GO TO 440
94:      KJ = NEQS*K-NEQS - (K*K+K)/2 + J
95:      GO TO 450
96:      KJ = NEQS*J-NEQS - (J*J+J)/2 + K
97:      GO TO ( 451, 452, 453, 454, 455, 451 ), IOPT
98:C
99:      451 A(KI) = ( (SNI+SNK)*A(KI) + (SNJ+SNK)*A(KJ) - SNK*BEST
100:      / (SNI + SNJ + SNK )
101:      GO TO 460
102:      452 A(KI) = (SNI*A(KI) + SNJ*A(KJ) ) / (SNI + SNJ)
103:      GO TO 460
104:      453 A(KI) = AMIN1( A(KI), A(KJ) )
105:      GO TO 460
106:      455 A(KI) = AMAX1 ( A(KI), A(KJ) )
107:      460 CONTINUE
108:C
109:      IF ( NGRPS *GT. 1 ) GO TO 200
110:C
111:      DO 610 K = 2, NEQS
112:      Z(K-1) = Z(K)
113:      IU(K-1) = IU(K)
114:      JU(K-1) = JU(K)
115:      Z(NEQS) = 0.0
116:      IU(NEQS) = 0
117:      JU(NEQS) = 0
118:      RETURN
119:C
120: 9000 PRINT 800

```



```

121: 800 FORMAT
122: 1(' SUBROUTINE GROUP. ALL VALUES OF OVERLAP VECTOR EXCEED 1.E35')
123: STOP
124: END

```

SOURCE LISTING FOR HIER-GRP SUBROUTINE STAGE

```

1:C-----
2:C
3:C SUBROUTINE STAGE
4:C-----
5:C
6:C THIS ROUTINE COMPUTES THE STAGE VALUES FOR PRINTING IN SUBROUTINE
7:C PRINTG. IT IS ASSUMED THAT THE PROPORTIONALITY ASSUMPTION IS SATISFIED
8:C BY THE PREDICTOR VARIABLES, OTHERWISE THE FORMULAS USED TO COMPUTE THE
9:C VALUES OF THE SRU AND ORU VECTORS ARE NOT VALID.
10:C-----
11:C
12:C

```

54

VARIABLE DESCRIPTIONS

```

13:C NEWS = NUMBER OF SYSTEMS.
14:C NPRED = NUMBER OF PREDICTOR VARIABLES.
15:C SA(I) = NUMBER OF CASES (OBSERVATIONS) IN SYSTEM I.
16:C SM(I) = CRITERION MEAN IN SYSTEM I.
17:C SSD(I) = CRITERION STANDARD DEVIATION IN SYSTEM I.
18:C B(IL) = STANDARD REGRESSION WEIGHT FOR PREDICTOR L IN SYSTEM I.
19:C WHERE IL = NPRED*(I-1) + L
20:C V(IL) = CRITERION CORRELATION WITH PREDICTOR L IN SYSTEM I.
21:C WHERE IL = NPRED*(I-1) + L
22:C IU(KU) = IDENT OF SYSTEM ABSORBING SYSTEM JU(KU) AT STAGE KU.

```

```

23:C JU(KU) = IDENT OF SYSTEM GROUPING WITH IU(KU) AT STAGE KU *
24:C SR(I) = R SQUARED OF SYSTEM I *
25:C ORU(KU) = R SQUARED FOR KU SYSTEMS AT STAGE KU *
26:C SRU(KU) = R SQUARED OF COMBINED SYSTEMS IU(KU),JU(KU) AT STAGE KU *
27:C KP(I) = IDENT OF SYSTEM FOLLOWING SYSTEM I IN FINAL
28:C HIERARCHICAL ORDERING.
29:C KU = NUMBER OF SYSTEMS AT KU STAGE, RANGES FROM NEQS-1 TO 1.
30:C -----
31:C
32: SUBROUTINE STAGE
33: I ( NEQS,NPREDS,SR,SM,SSD,B,V,IU,JU,SR,ORU,SRU, KP )
34:C INPUT * * * * *
35:C OUTPUT ----- UNCHANGED * * * *
36:C
37: DIMENSION, SR(I),SSD(I),R(I),IU(I),SR(I),ORU(I),KP(I)
38: I ,SR(I), V(I), JU(I), SRU(I)
39:C
40: ON = 0.0
41: SUMX = 0.0
42: SUMY = 0.0
43: SUMR = 0.0
44: IL = 0
45: DO 120 I = 1, NEQS
46: KP(I) = 0
47: ON = ON + SR(I)
48: SUMX = SUMX + SR(I) * SM(I)
49: SUMY = SUMY + SR(I) * ( SSD(I)**2 + SM(I)**2 )
50: SUMR = 0.0
51: DO 110 L = 1, NPREDS
52: IL = IL + 1
53: 110 SUMRV = SUMRV + R(IL) * V(IL)
54: SR(I) = SUMRV
55: 120 SUMR = SUMR + SR(I) * ( SSD(I)**2 + SUMRV + SM(I)**2 )
56: OMSQ = ( SUMX / ON ) ** 2
57: OSSQ = SUMY / ON - OMSQ
58: ORU(NEQS) = ( SUMR / ON - OMSQ ) / OSSQ

```

```

59: SRU(NEWS) = 0.0
60: KU = NEWS - 1
61: C
62: 200 SUMRIJ = 0.0
63: IK = JU(KU)
64: JK = TU(KU)
65: C
66: 300 RSWI = SM(IK)
67: IF ( KP(IK) .EQ. 0 ) GO TO 400
68: KI = KU + 1
69: DO 320 K = KI, NEWS
70: IF ( TU(K) - IK ) 320, 330, 320
71: CONTINUE
72: GO TO 9000
73: 330 RSWI = SRU(K)
74: C
75: 400 SWI = 0.0
76: SUMI = 0.0
77: SUMISW = 0.0
78: I = IK
79: 410 SWI = SWI + SR(I)
80: SUMI = SUMI + SN(I) * SM(I)
81: SUMISW = SUMISW + SN(I) * (SSD(I)**2 + SM(I)**2)
82: J = JK
83: 420 SUMBV = 0.0
84: IN = NPRED5 * (I-1)
85: JN = NPRED5 * (J-1)
86: DO 430 L = 1, NPRED5
87: IL = L + IN
88: JL = L + JN
89: 430 SUMBV = SUMBV + B(IL) * V(JL)
90: SUMRIJ = SUMRIJ + SN(I)*SN(J) * SSD(I)*SSD(J) * SUMBV
91: J = KP(J)
92: IF ( J .GT. 0 ) GO TO 420
93: IF ( KP(I) .EQ. 0 ) GO TO 500
94: I = KP(I)

```

```

95:      GO TO 410
96:C
97: 500 IF ( JK *EQ* JU(KU) ) GO TO 600
98:      SNJ = SNI
99:      SUMJ = SUMI
100:      SUMJSW = SUMISW
101:      RSQJ = RSQI
102:      IK = IU(KU)
103:      JK = JU(KU)
104:      GO TO 300
105:C
106: 600 KP(1) = JK
107:      SUMKI = RSQI * ( SNI * SUMISW - SUMI**2 )
108:      SUMKJ = RSQJ * ( SNJ * SUMJSW - SUMJ**2 )
109:      SUMR = SUMR + ( SUMRIJ + 2.0 * SUMI * SUMJ
110:      1 - SNJ * (SUMRI + SUMI**2) / SNI
111:      2 - SNI * (SUMRJ + SUMJ**2) / SNJ ) / (SNI + SNJ)
112:      ORU(KU) = (SUMR / ORU - ORU) / USSQ
113:      SRU(KU) = ( SUMRIJ + SUMRI + SUMRJ ) /
114:      1 ((SNI+SNJ)*(SUMISW + SUMJSW) - (SUMI+SUMJ)**2 )
115:      KU = KU - 1
116:      IF ( KU *GT* 0 ) GO TO 200
117:C
118:      RETURN
119:C
120: 9000 PRINT 800
121: 800 FORMAT ( ' SUBROUTINE STAGE. ABSORBING SYSTEM NOT FOUND.' )
122:      STOP
123:      END

```


SOURCE LISTING FOR HIER-GNP SUBROUTINE PRINTG

```

1:C-----
2:C
3:C SUBROUTINE PRINTG
4:C-----
5:C
6:C THIS PROGRAM PRINTS THE GROUPING REPORT. OUTPUT INCLUDES A LIST
7:C OF THE ORIGINAL SYSTEMS TOGETHER WITH THEIR RSQ'S. AT EACH STEP OF THE
8:C GROUPING PROCEDURE, THE SYSTEMS GROUPED, THE DECISION VALUE AND THE F-
9:C STATISTIC ARE PRINTED. IN ADDITION A SUMMARY ROSTER GIVING ALL THE
10:C SYSTEMS AND THEIR MEMBERS IS PRINTED. THE INFORMATION PRINTED BY THIS
11:C SUBROUTINE DEPENDS HEAVILY ON THE PROPORTIONALITY ASSUMPTION FOR ITS
12:C CORRECTNESS. IN PARTICULAR, ALL SYSTEMS RSQ'S EXCEPT THE NEQS SYSTEMS
13:C RSQ AND THE NEQS INITIAL SYSTEMS RSQ'S ARE INCORRECT IF THE PROPORTION-
14:C ALITY ASSUMPTION DOES NOT HOLD. THIS IN TURN INVALIDATES THE F-TESTS,
15:C AND THE ORDER OF GROUPING IF GROUPING OPTIONS 1 OR 6 ARE USED.
16:C-----
17:C
18:C
19:C IOPT = GROUPING OPTION NO. (1 THRU 6) USED TO PRINT OBJECTIVE
20:C FUNCTION DESCRIPTION AFTER REPORT HEAD.
21:C NEQS = NUMBER OF SYSTEMS BEFORE GROUPING (AT NEQS STAGE).
22:C NPRED = NUMBER OF PREDICTORS IN EACH SYSTEM.
23:C SN(I) = NUMBER OF CASES IN SYSTEM I AT NEQS STAGE.
24:C R (IL) = BETA WEIGHT FOR PREDICTOR L IN SYSTEM I.
25:C WHERE IL = NPRED*(I-1) + L.
26:C PM(L) = MEAN FOR PREDICTOR L.
27:C PSD(L) = STANDARD DEVIATION FOR PREDICTOR L.
28:C IU (KU) = IDENT OF SYSTEM ABSORBING SYSTEM JU(KU) AT KU STAGE.
29:C JU (KU) = IDENT OF SYSTEM GROUPING WITH IU(KU) AT KU STAGE.
30:C Z (KU) = DECISION VALUE CAUSING THE SELECTION OF IU(KU), JU(KU).
31:C SR (I) = R SQUARED OF SYSTEM I.
32:C GRU (KU) = R SQUARED FOR KU SYSTEMS AT KU STAGE.
33:C SPU (KU) = R SQUARED OF COMBINED SYSTEMS IU(KU),JU(KU) AT KU STAGE.
34:C KS (J) = KU WHERE J= JU(KU)

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VARIABLE DESCRIPTIONS

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35:C KP ( I ) = IDENT OF SYSTEM FOLLOWING SYSTEM I IN FINAL
36:C HIERARCHICAL ORDERING.
37:C KO ( ) = SYSTEM IDENTIS IN FINAL HIERARCHICAL ORDERING.
38:C A ( ) = WORK AREA
39:C BE ( ) = WORK AREA, USED TO STORE BETA WEIGHTS FOR STEPWISE PRINTING
40:C KU = NUMBER OF SYSTEMS AT KU STAGE, RANGES FROM NEQS-1 TO 1.
41:C RCONST = REGRESSION CONSTANT.
42:C-----
43:C
44:
45: SUBROUTINE PRINTG
46:C 1N * * * * *
47:C OUT -----UNCHANGED-----
48:C
49: 2 KS,KP,KO,A,BE)
50:C OUT * * * * W
51: DIMENSION SNI( ), SM( ), SSD( ), Z( ), JU( ), ORU( ), KS( ), KO( ),
52: 1 IU( ), SR( ), SRU( ), KP( ), A( ), BE( )
53: 2 ,R( ), PH( ), PSD( )
54:C
55: 1 FORMAT ( / 45H MAXIMIZED DECISION VALUE = ORU(KU+1)-ORU(KU) )
56:C
57: 2 FORMAT(/125H MAXIMIZED DECISION VALUE = AVERAGE OF ALL SNI(KU)*SNJ
58: 1(KU) VALUES OF ORU(NEQS)-ORU(NEQS-1) BETWEEN SYSTEMS IU(KU) AND JU
59: 1(KU). )
60:C
61: 3 FORMAT ( /123H MAXIMIZED DECISION VALUE = MINIMUM OF ALL (NU(KU))*
62: 12-NU(KU) )/2 VALUES OF ORU(NEQS)-ORU(NEQS-1) WITHIN NEW SYSTEM IU(
63: 2KU). )
64:C
65: 4 FORMAT(/125H MINIMIZED DECISION VALUE = AVERAGE OF ALL SNI(KU)*SNJ
66: 1(KU) VALUES OF ORU(NEQS)-ORU(NEQS-1) BETWEEN SYSTEMS IU(KU) AND JU
67: 2(KU). )
68:C
69: 5 FORMAT ( /123H MINIMIZED DECISION VALUE = MAXIMUM OF ALL (NU(KU))*
70: 12-NU(KU))/2 VALUES OF ORU(NEQS)-ORU(NEQS-1) WITHIN NEW SYSTEM IUK

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71:      2U) . )
72:C
73:      6 FORMAT ( / 45H MINIMIZED DECISION VALUE = ORU(KU+1)-ORU(KU) )
74:C
75:      7 FORMAT( 8X 116H
76:      1KU) AT KU+1 STAGE.
77:C
78:      8 FORMAT( 8X 116H
79:      1 IU(KU) AT KU STAGE.
80:C
81:      9 FORMAT( 8X 116H
82:      1N JU(KU) AT KU STAGE.
83:C
84:      10 FORMAT( 7X 52H
85:      1 /8X 116H
86:      2KU STAGE.
87:C
88:      11 FORMAT ( / 43H
89:      1 // 15, 22H INITIAL SYSTEMS RSQ = F7.4
90:      2 // 10( 12H SYS PSW ))
91:C
92:      12 FORMAT(1X,126(1H*))// STAGE = ,13, OVERALL RSQ = ,F7.4,12X,*,*,*//
93:      146X,*,*,14X,*F-TEST FOR THE EQUALITY OF REGRESSION PARAMETERS*//
94:      127X,*SYSTEMS*,12X,*,*,/22X,*GROUPING THIS STAGE *,*//
95:      2* FOR SYS**S COMBINED AT THIS STAGE*,
96:      3* FOR SYS**S COMBINED UP TO THIS STAGE*,19(1H-),* * ,
97:      432(1H-),3X,35(1H-)/20X,*SYS NO. NO.,9X,*,*,10X,
98:      5*CHANGE FROM*,25X,*CHANGE FROM*/19X,*IDENT MEMBERS CASES RSQ*,
99:      6* *,10X,13,*SYSTEMS RESIDUAL*,13X,13,*SYSTEMS RESIDUAL*//
100:      719X,13,17,19,F6.4,* * RSQ*,F12.4,F13.4,8X,*RSQ*,F12.4,F13.4//
101:      819X,13,17,19,F6.4,* * DF*,112,113,9X,*DF*,112,113/46X,*,*,*//
102:      919X,*DECISION VALUE=*,F10.4,* * FSTAT=*,F8.2,* SIG LVL=*,F6.4,
103:      17X,*FSTAT=*,F8.2,* SIG LVL=*,F6.4//36X,*SYSTEMS SUMMARY RSQ*,
104:      236X,22(1H-)/14X,*STAGE SYS NO. NO. * SYS*//
105:      3 14X,*IDENT LOSS MEMBERS RSQ CASES * IDENT *,
106:      4*IDENTIFICATION OF OTHER MEMBERS*)

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107:C
108: 13 FORMAT(14X,13,F7.4,15,F7.4,17, , ,14,14,2014,9(/40X, , ,5X,2014))
109:C
110: 14 FORMAT(40X, , , /40X, , ,5X, , ,BETA WEIGHTS FOR THE NEW SYSTEM,
111: 1 14,8X, ,NEW SYS CRITERION MEAN = ,F9.4/46X, , ,5X,35(1H-),
112: 2 8X, ,NEW SYS CRITERION SD = ,F9.4/46X, , ,1018)
113:C
114: 15 FORMAT(46X, , ,10F8.4, 20(/40X, , ,10F8.4) )
115:C
116: 16 FORMAT(46X, , , /46X, , , RAW SCORE WEIGHTS FOR THE NEW SYSTEM,
117: 1 14,10X, ,REGRESSION CONSTANT = ,F9.4/46X, , , ,
118: 2 40(1H-)/46X, , ,5116)
119:C
120: 117 FORMAT(46X, , ,5F16.4, 20(/40X, , ,5F16.4))
121:C
122: 17 FORMAT(/14X,13, , SINGLE MEMBER SYSTEMS,2014, 9(/39X,2014) )
123:C
124:911 FORMAT( 10(15,F7.4) )
125:C
126: TOT =0.0
127: DO 50 I=1,NEQS
128: 50 TOT = TOT +SN(I)
129: NTOT =TOT
130:C
131: PRINT 90
132: 90 FORMAT ( 1H2 / 1H1 )
133: PRINT 91
134: 91 FORMAT(/ , 111. HIERARCHICAL GROUPING RESULTS, /6X,29(1H-))
135:C
136: 115 GO TO ( 121, 122, 123, 124, 125, 126 ), 10PT
137:C
138: 121 PRINT 1
139: GO TO 160
140: 122 PRINT 2
141: PRINT 7
142: PRINT 9

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143:      GO TO 160
144: 123 PRINT 3
145: PRINT 8
146: PRINT 9
147:      GO TO 160
148: 124 PRINT 4
149: PRINT 7
150: PRINT 9
151:      GO TO 160
152: 125 PRINT 5
153: PRINT 8
154: PRINT 9
155:      GO TO 160
156: 126 PRINT 6
157: C
158: 160 PRINT 10
159: C
160: 200 DO 210 K = 1,NEWS
161: KS(K) = K+1
162: KP(K) = 0
163: 210 A(K) = SR(K)
164: KS(NEWS) = 0
165: PRINT 11, 10PT,NEWS,ORU(NEWS)
166: PRINT 911,1,1, SR(1), 1 = 1,NEWS )
167: KU = NEWS - 1
168: DF2X = NTOT - NEWS * (NPRED5 + 1)
169: IF ( ORU(NEWS) .GT. 1. ) ORU(NEWS) = 1.
170: RES = 1. - ORU(NEWS)
171: C
172: C
173: 300 KUP1 = KU + 1
174: IF ( ORU(KU) .GT. ORU(KUP1) ) ORU(KU) = ORU(KUP1)
175: DI = ORU(KUP1) - ORU(KU)
176: ODI = ORU(NEWS) - ORU(KU)
177: RES1 = 1. - ORU(KUP1)
178: DF1X = (NEWS - KU) * (NPRED5 + 1)

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179:      ID = IU(KU)
180:      JD = JU(KU)
181:      I = ID
182:      310      IF ( KS(I).EQ. JU ) GO TO 330
183:      I = KS(I)
184:      GO TO 310
185:      330      KS(I) = KS(JD)
186:      KS(JD) = KU
187:      I = ID
188:      NI = I
189:      SHI = SH(I)
190:      340      IF ( KP(I) .EQ. U ) GO TO 360
191:      I = KP(I)
192:      NI = NI + 1
193:      SHI = SHI + SH(I)
194:      GO TO 340
195:      360      KP(I) = JU
196:      J = JD
197:      NJ = I
198:      SNJ = SH(J)
199:      370      IF ( KP(J) .EQ. U ) GO TO 390
200:      J = KP(J)
201:      NJ = NJ + 1
202:      SNJ = SNJ + SH(J)
203:      GO TO 370
204:      390      NSI = SHI
205:      NSJ = SNJ
206:      DF1 = UPRED5+1
207:      DF2 = NTOT - KUPI*(UPRED5+1)
208:      F = (OI*DF2)/(DF1*RES1)
209:      F1 = (ODI*DF2X)/(DF1X*RES)
210:      IF1=DF1
211:      IF2=DF2
212:      IF1X=DF1X
213:      IF2X=DF2X
214:      CALL PLEVEL( DF1, DF2, F, PRED)

```

```

215: CALL PLEVEL( DFIX, DFZX, FI, PROBI)
216: PRINT 12,
217: 1 KU, ORU(KU), KUPI, NEWS, ID, NI, ISI, A(ID), DI, RESI, ODI, RES,
218: 2 JD, IJ, NSJ, A(JJ), IF1, IF2, IFIX, IFZX,
219: 3 Z(KU), F, PROB, FI, PROBI
220: A(ID) = SRU(KU)
221: MIT = NEQS - KU + 2
222: KOW = MIT - 1
223: I = 1
224: C
225: 400 IF ( KP(I) * GI * U ) GO TO 410
226: KOW = KOW + 1
227: KU(KOW) = I
228: GO TO 440
229: 410 NI = 1
230: KU(NI) = I
231: SNI = SU(I)
232: SLOSS = 0.0
233: IGRUP = NEWS
234: J = KF(I)
235: IF ( I * NE * ID ) GO TO 420
236: C INITIALIZE BETA WEIGHT COMPUTATION
237: SUMX = SN(I) * SM(I)
238: SUMX2 = SN(I) * (SSD(I)**2 + SM(I)**2)
239: CONST = SN(I) * SSD(I)
240: IK = (I-1) * UPREDS
241: DO 412 K = 1, UPREDS
242: IK = IK + 1
243: 412 RE(K) = B(IK) * CONST
244: KUJ = KS(J)
245: SLOSS = SLOSS + (ORU(KUJ + 1) - ORU(KUJ)
246: IF ( KUJ * GI * IGRUP ) GO TO 426
247: IGRUP = KUJ
248: 426 NI = NI + 1
249: SNI = SNI + SM(J)
250: KU(MI) = J

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251: IF ( I .LE. ID ) GO TO 429
252:C ACCUMULATE BETA WEIGHTS FOR THIS STAGE
253: SUMX = SUMX + SM(J) * SM(J)
254: SUMX2 = SUMX2 + SM(J) * ( SM(J)**2 + SM(J)**2 )
255: CONST = SM(J) * SM(J)
256: IK = (J-1) * NPRED5
257: DO 428 K = 1, NPRED5
258: IK = IK + 1
259: BE(K) = BE(K) + B(IN)*CONST
260: 429 J = KP(J)
261: IF ( J .GT. 0 ) GO TO 420
262: 430 NSI = SNI
263: PRINT 13, IGRUP, SLUSS,
264: I NI, A(1), NSI, ( NO(K), K = 1, NI )
265: IF ( I .LE. ID ) GO TO 440
266:C COMPUTE AND PRINT SYSTEM MEAN, SD, BETA WEIGHTS
267: SUMX = SUMX / SNI
268: SUMX2 = SQR ( SUMX2/SNI - SUMX**2 )
269: CONST = 1. / (SNI * SUMX2)
270: DO 435 K = 1, NPRED5
271: 435 BE(K) = BE(K) * CONST
272: MIN = MIND ( 10, NPRED5 )
273: PRINT 14, ID, SUMX, SUMX2, ( K, K = 1, MIN )
274: PRINT 15, ( BE(K), K = 1, NPRED5 )
275:C COMPUTE AND PRINT RAW SCORE WEIGHTS AND REGRESSION CONSTANT
276: SUM = 0
277: DO 437 K = 1, NPRED5
278: BE(K) = BE(K) * SUMX2 / PSD(K)
279: 437 SUM = SUM + BE(K) * PM(K)
280: RCONST = SUMX - SUM
281: MIN = MIND ( 5, NPRED5 )
282: PRINT 16, ID, RCONST, ( K, K = 1, MIN )
283: PRINT 17, ( BE(K), K = 1, NPRED5 )
284: 440 I = KS(I)
285: IF ( I .GT. 0 ) GO TO 400
266:C

```



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287:      IF ( KOW .LT. MIT ) GO TO 520
288:      NKOW = KOW - MIT + 1
289:      PRINT 17
290:      1 , NKOW, ( KO(K), K = MIT, KOW )
291:      520 KU = KU - 1
292:      IF ( KU .GT. 0 ) GO TO 300
293:      C
294:      PRINT 421
295:      421 FORMAT ( / 47H .....
296:      1 58H .....
297:      2 27H ..... / )
298:      RETURN
299:      C
300:      END

```

SOURCE LISTING FOR HIER-GRP SUBROUTINE PLEVEL

```

1:      C
2:      SUBROUTINE PLEVEL (XDF1,XDF2,F,P)
3:      DIMENSION Y(6),ARG(3),GANA(3)
4:      BASHLN(Z,X)=(X+.5)*ALOG(X)-X+.918938534+(.833333333E-1-2*(.2777777
5:      178E-2-2*(.793650794E-3-2*(.595238095E-3-2*(.841750842E-3))))/X
6:      DF1=XDF1
7:      GF2=XDF2
8:      IF(DF1 .GT. 1000.)DF1=1000.
9:      IF(DF2 .GT. 1000.)DF2=1000.
10:     IF(DF1.LT.1..OR.DF2.LT.1..OR.F.LT.0.)GO TO 14
11:     IF(ARG(1).EQ.DF1.AND.ARG(2).EQ.DF2)GO TO 7
12:     ARG(1) = DF1
13:     ARG(2) = DF2
14:     ARG(3) = DF1+DF2

```

```

15:      DO 6 I=1,3
16:      IF(ARG(I).EQ.1.)GO TO 5
17:      T = ARG(I)-2.
18:      J = AMOD(ARG(I),2.)+1.
19:      GO TO (2,I),J
20:      1 U = (T-1.)*.5
21:      GAMA(I) = .572364943-T*.693147181
22:      IF(U.LT.2.)GO TO 25
23:      GO TO 3
24:      2 T = T*.5
25:      GAMA(I) = J.
26:      25 IF(T.LT.2.)GO TO 6
27:      GO TO 4
28:      3 Z = 1./(U*U)
29:      GAMA(I) = GAMA(I)-.645484(Z,U)
30:      4 Z = 1./(T*T)
31:      GAMA(I) = GAMA(I)+.645484(Z,T)
32:      GO TO 6
33:      5 GAMA(I) = .572364943
34:      6 CONTINUE
35:      C = GAMA(1)+GAMA(2)-GAMA(3)-.693147181
36:      Y(1) = .4054651181
37:      Y(2) = -1.203972804
38:      Y(3) = .5877866649
39:      Y(4) = Y(2)
40:      Y(5) = Y(1)
41:      7 AX = DF2/(F*DF1+DF2)
42:      IF (AX.GT.0.99999900) GO TO 136
43:      8 = ATANH(SQRT(AX/(1.-AX)))/50.
44:      IF(H.LE..130899694E-1)GO TO 8
45:      H = .261799387E-1-H
46:      CN = DF1-1.
47:      CH = (DF2-1.)*.5
48:      P = -1./H
49:      XM = -H
50:      GO TO 9

```

```

51: 5 C4 = DF2-1.
52: C4 = (DF1-1.)*.5
53: P = 0.
54: XH = H
55: 9 IF (C4*DE*0.) GO TO 95
56: XX = Y(2)-C
57: IF (XX*LT*0.) GO TO 95
58: P=P+EXP(XX*69.)
59: Y(6) = -.5106256236
60: X = 0.
61: 90 13 I=1,10
62: 90 10(11,11,11,11,11,11,11,11,11,11,10),1
63: 12 Y(6) = Y(2)
64: 11 90 13 J=1,5
65: X = X+H
66: X5 = 514(X)
67: Z = Y(J)-C+CN*ALOG(X5)+C4*ALOG(1.-X5*X5)
68: IF(Z)15,12,12
69: 12 P = P+EXP(Z*69.)
70: 13 CONTINUE
71: P = X4*P
72: IF (P*LT*.1*DE*05 ) P = 0.
73: 135 RETURN
74: 136 P = 1.
75: 90 TO 135
76: 14 P = 1.
77: PRINT15,DF1,DF2,F
78: 15 FORMAT(741)DF1 = F5,J,H,DF2 = F5,J,5H,F = F10.5//
79: 148H P DOES NOT EXIST IF DF1 OR DF2 IS LESS THAN 1 /
80: 248H OR IF F IS LESS THAN ZERO. /
81: 348H P FOR THIS PROBLEM HAS BEEN ARBITRARILY SET /
82: 448H EQUAL TO 1. AND A NORMAL RETURN HAS OCCURED. )
83: 90 TO 135
84: END

```